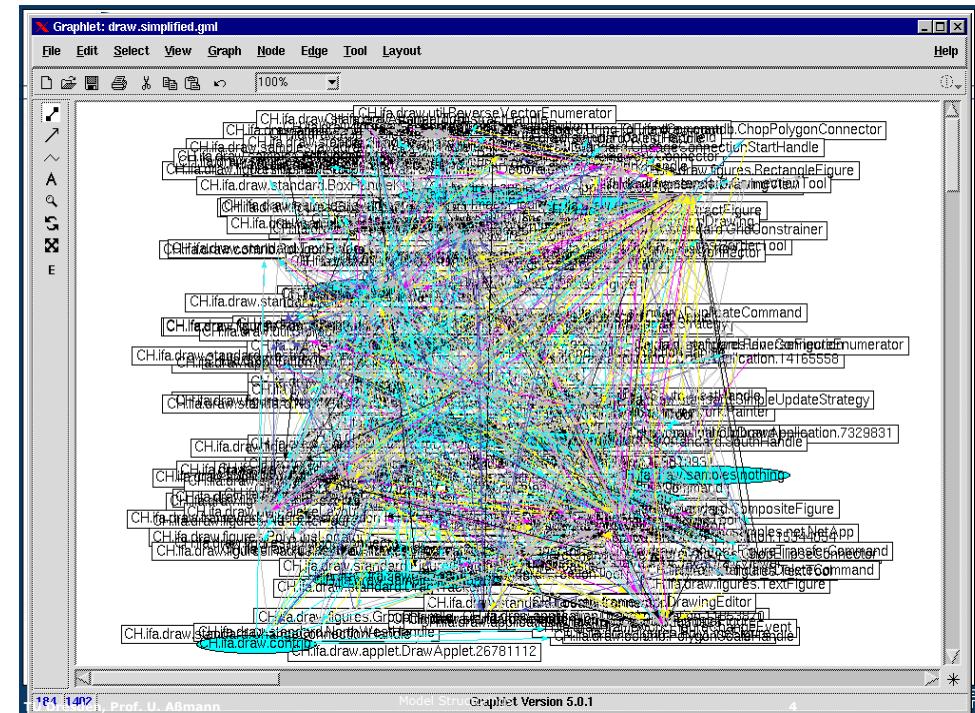
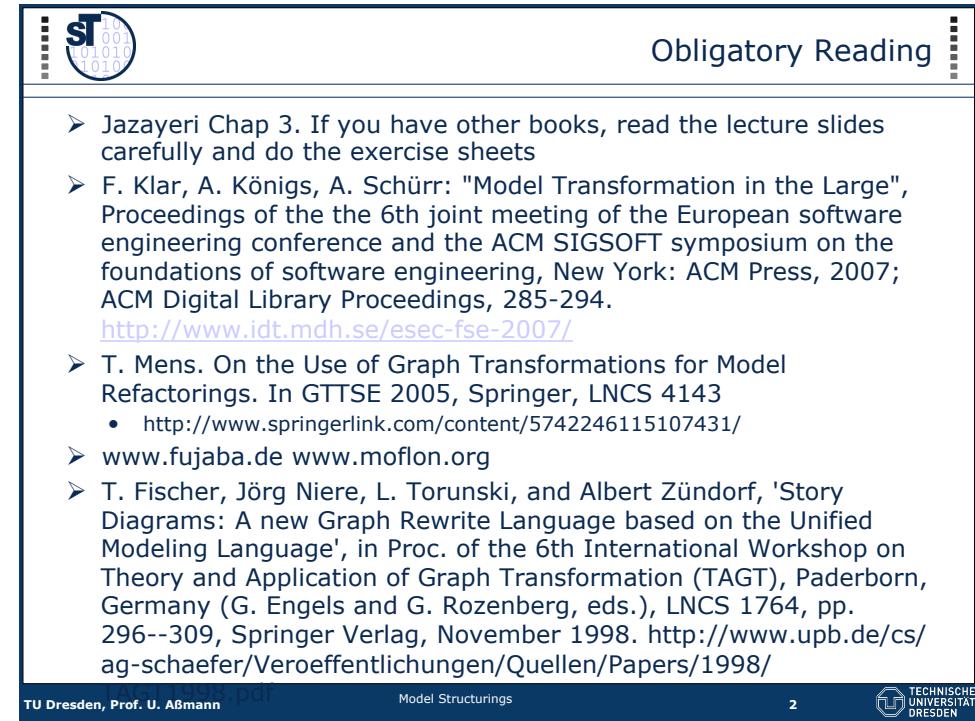
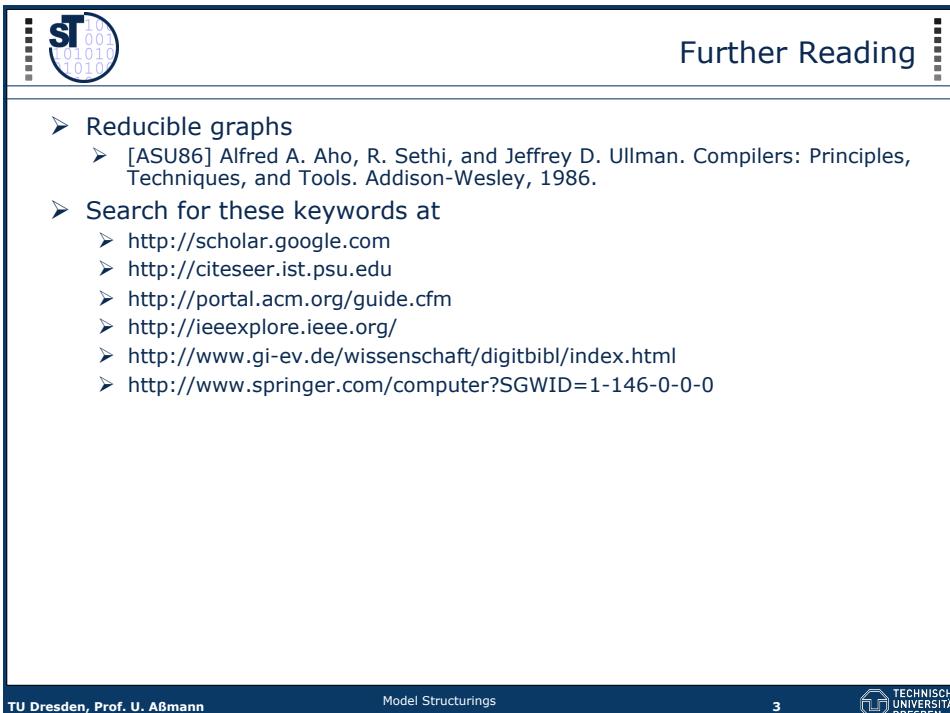


# 14. How to Transform Models with Graph Rewriting

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Version 11-0-2, 10.12.11

1. Graph Structurings with Graph Transformations
  2. Additive and Subtractive GRS (external)
  3. Triple Graph Grammars
  4. (Graph Structurings split off into chap. 16)





## The Problem: How to Master Large Models

- Large models have large graphs
- They can be hard to understand
  
- Figures taken from Goose Reengineering Tool, analysing a Java class system [Goose, FZI Karlsruhe]



## Answer: Simon's Law of Complexity

- H. Simon. The Architecture of Complexity. Proc. American Philosophical Society 106 (1962), 467-482. Reprinted in:
- H. Simon, The Sciences of the Artificial. MIT Press. Cambridge, MA, 1969.

**Hierarchical structure reduces complexity.**

**Herbert A. Simon, 1962**



## Problems



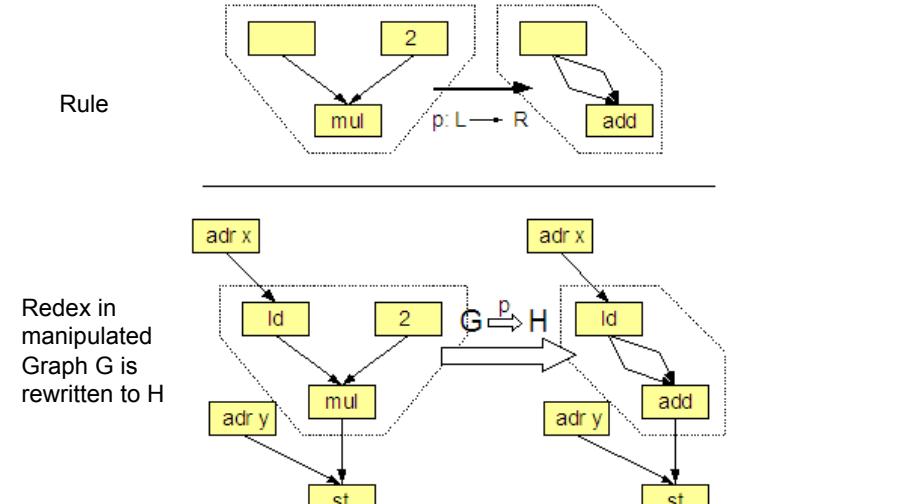
- Question: How to Treat the Models of a big Swiss Bank?
  - 25 Mio LOC
  - 170 terabyte databases
- Question: How to Treat the Models of a big Operating System?
  - 25 Mio LOC
  - thousands of variants
- Requirements for Modelling in Requirements and Design
  - We need automatic structuring methods
  - We need help in restructuring by hand...
- Motivations for structuring
  - Getting better overview
  - Comprehensibility
  - Validatability, Verifyability



# 14.1 GRAPH TRANSFORMATIONS

- Once, we do not only manipulate edges, but also nodes, we leave the field of Edge Addition Rewrite Systems
- We arrive at general Graph Rewrite Systems (GRS)
  - Transformation of complex structures to simple ones
  - Structure complex models and systems

## GRS Example

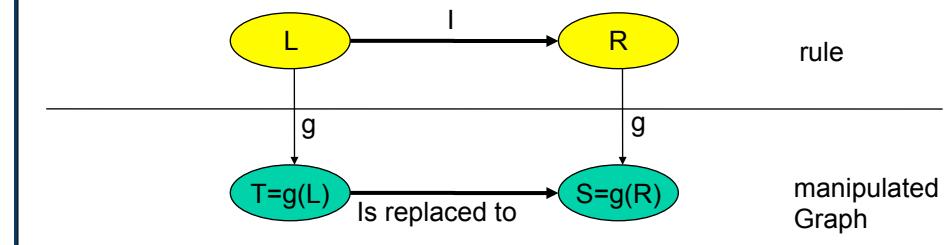


## Graph Rewrite Systems

- A *graph rewrite system*  $G = (S)$  consists of
  - A set of rewrite rules  $S$ 
    - A rule  $r = (L, R)$  consists of 2 graphs  $L$  and  $R$  (left and right hand side)
    - Nodes of left and right hand side must be identified to each other
    - $L$  = "Mustergraphen";  $R$  = Ersetzungsgraph"
  - An application algorithm  $A$ , that applies a rule to the manipulated graph
    - There are many of those application algorithms...
- A *graph rewrite problem*  $P = (G, Z)$  consists of
  - A graph rewrite system  $G$
  - A start graph  $Z$
  - One or several result graphs
  - A derivation under  $P$  consists of a sequence of applications of rules (direct derivations)
- GRS offer automatic graph rewriting
  - A GRS applies a set of Graph rewrite rules until nothing changes anymore (to the fixpoint, chaotic iteration)
  - Problem: Termination and Uniqueness of solution not guaranteed

## Application of a Graph Rewrite Rule

- **Match** the left hand side: Look for a subgraph  $T$  of the manipulated graph: look for a graph morphism  $g$  with  $g(L) = T$
- Evaluate **side conditions**
- Evaluate right hand side
  - Delete all nodes and edges that are no longer mentioned in  $R$
  - Allocate new nodes and edges from  $R$ , that do not occur in  $L$
- **Embedding:** redirect certain edges from  $L$  to new nodes in  $R$ 
  - Resulting in  $S$ , the mapping of  $g(R)$





## PROGRES, the GRS tool from the IPSEN Project

- PROGRES is a wonderful tool to model graph algorithms by graph rewriting
- Textual and graphical editing
- Code generation in several languages
  
- [http://www-i3.informatik.rwth-aachen.de/tikiwiki/tiki-index.php?page\\_ref\\_id=213](http://www-i3.informatik.rwth-aachen.de/tikiwiki/tiki-index.php?page_ref_id=213)

This example illustrates the possibilities of PROGRES to define *parametrized productions*, which must be instantiated (in the series of a procedure call) with actual attribute values and node types. In this way, a single production may abstract from a set of productions which differ only with respect to used attribute values and types of matched or created nodes. In almost all cases, node type parameters are not used for matching purposes, but provide concrete types for new nodes of the right-hand side.

```
production CreateModule ( Mname : string; InterfaceDescription : file;
                         Mtype : type_is MODULE ) =
    [1 : System] --> [2 : MODULE]
    name(Mname)
    type(Mtype)

    transfer [2' : Name := Mname;
              2' : File := InterfaceDescription];
    end;

production DeleteModule ( Mname : string ) =
    [1 : MODULE] --> []
    has(name(Mname))
    needs([2 : VARIANT])
    type(VARIANT)

    transfer [1' : Name := Mname];
    end;

production ChangeModuleType ( Mname : string; NewType : type_is MODULE ) =
    [1 : MODULE] --> []
    name(Mname)

    transfer [1' : NewType];
    end;

embedding redirect <-uses->, <-has->, <-contains->;
transfer [1' : Name := 1' : Name;
          1' : File := 1' : File];
end;
```

Fig. 12: Specification of basic graph transformations

```
query ConfigurationConsistency( out QName : string ) =
    /* A configuration is consistent if:
     * 1) it contains a variant of the system's main module, */
    /* 2) it contains a variant for any module which is
     *     needed by another included variant, and */
    /* 3) it does not contain variants which are not needed */
    /* by needed variants. */

use LocalName: string do
    ConfigurationWithMain( out LocalName )
    & not UnresolvedImportExists( LocalName )
    & not ConfigurationWithUselessVariant( LocalName )
    & QName := LocalName
end;
```

```
end;
test ConfigurationWithMain( out QName : string ) =
    [1 : System] --> [3 : MODULE]
    contains
    has
    [2 : Config] --> [4 : VARIANT]
    domains
    name(QName)
```

```
end;
test UnresolvedImportExists( QName : string ) =
    [1' : VARIANT] --> [3 : MODULE]
    needs
    [2 : Config] --> [4 : VARIANT]
    contains
    name(QName)
```

```
end;
test ConfigurationWithUselessVariant( QName : string ) =
    [1 : System] --> [3 : MODULE]
    contains
    has
    [2 : Config] --> [4 : VARIANT]
    domains
    [5 : MODULE] --> [6 : VARIANT]
    needs
    contains
    name(QName)
```

```
production CreateModule ( ClientModuleName, ServerModuleName : string ) =
    [1 : MODULE] --> [2 : MODULE]
    depends
    name(ClientModuleName)
    name(ServerModuleName)
```

```
end;
production InitConfig( QName : string;
                        NewProps : string[0..n];
                        OldProps : string[0..n] ) =
    [1 : System] --> [3 : MODULE]
    contains
    [2 : Config] --> [4 : VARIANT]
    has
    [1' : MODULE] --> [3' : MODULE]
    contains
    name(QName)
    name(QName)
```

```
end;
condition '4.Props >= 1' RedProps;
transfer [2' : Name := QName;
          2' : Props := RedProps];
return RedProps := merge(RedProps, '4.Props');
```

Fig. 14: Specification of additionally needed complex productions

## Type Scheme of a Graph

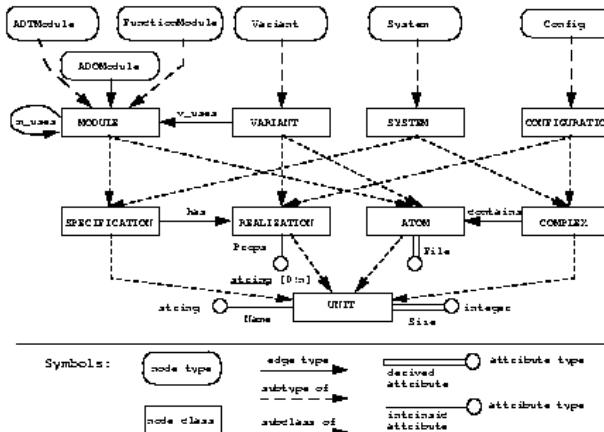


Fig. 5: The graph schema of MIL graphs (without derived relationships)

- Boxes with round corners represent node types which are connected to their uniquely defined classes by means of dashed edges representing “type is instance of class” relationships; the type ADTModule belongs for instance to the class MODULE.
- Solid edges between node classes represent edge type definitions; the edge type v\_uses is for instance a relationship between VARIANT nodes and MODULE nodes and m\_uses edges connect MODULE nodes with other MODULE nodes.
- Circles attached to node classes represent attributes with their names above or below

## Different Kinds of Graph Transformation Systems

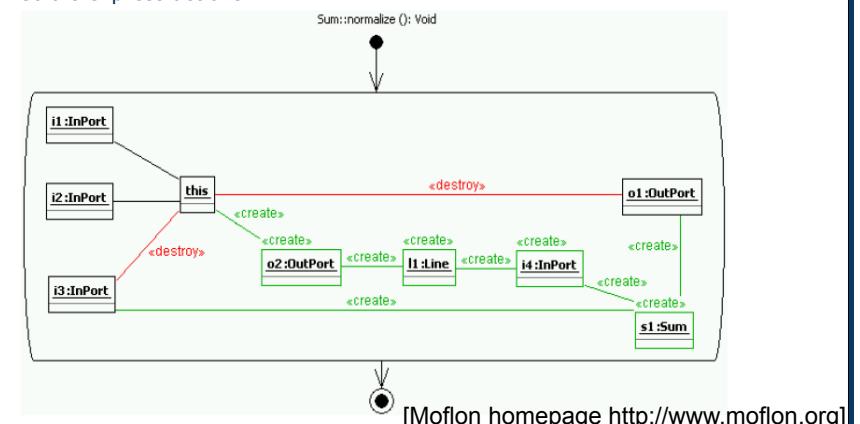
- Automatic Graph Rewriting
  - Iteration of rules until termination
- Programmed Graph Rewriting
  - The rules are applied of a control flow program. This program guarantees termination and selects one of several solutions
  - Examples: PROGRES from Aachen/München
  - Fujaba on UML class graphs, from Paderborn, Kassel [www.fujaba.de](http://www.fujaba.de)
  - MOFLON from Darmstadt [www.moflon.org](http://www.moflon.org)
- Graph grammars
  - Special variant of automatic graph rewrite systems
  - Graph grammars contain in their rules and in their generated graphs special nodes, so called non-terminals
  - A result graph must not have non-terminals
  - In analogue to String grammars, derivations can be formed and derivation trees

## Different Kinds of Transformation Systems: TRS and DAGRS

- Term rewriting replaces terms (ordered trees)
  - right and left hand sides are Terms
- Ground term rewrite systems, GTRS: only ground terms in left hand sides
  - A GTRS always works bottom-up on the leaves of a tree
  - For GTRS there are very fast, linear algorithms
- Variable term rewrite systems, VTRS: terms with variables
  - Replacement everywhere in the tree
- Dag rewrite systems (DAGRS)
  - If a term contains a variable twice (non-linear), it specifies a dag
  - Dag rewrite systems contain dags in left and right hand sides (non-linear term rewriting)

## MOFLON and Fujaba

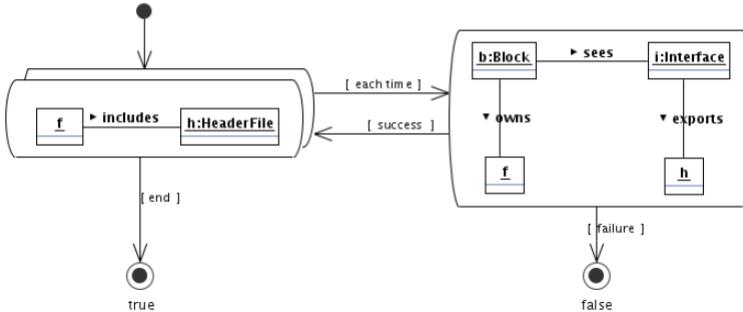
- MOFLON and Fujaba embed graph rewrite rules into activity diagrams (aka storyboards)
  - A rule set executes as an atomic activity
  - Colors express actions



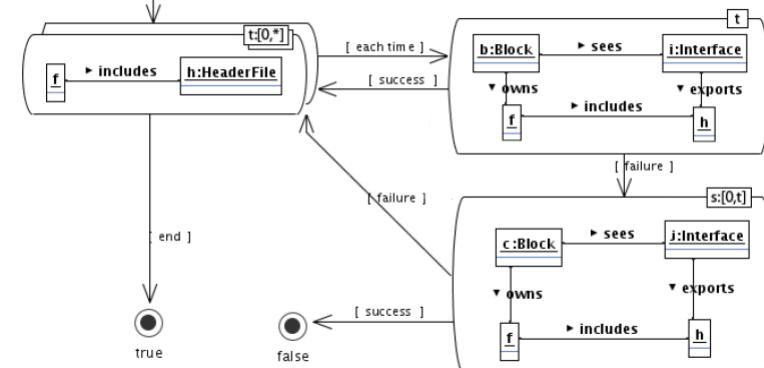
[Moflon homepage <http://www.moflon.org>]

## Storyboards are Refined Activity Diagrams

Analyzer::areAllIncludesValid (f: File): Boolean

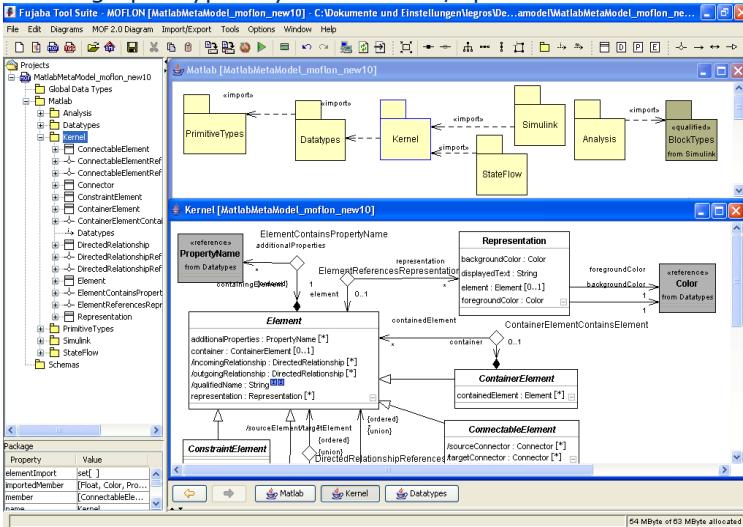


Analyzer::isIncludeStable (f: File): Boolean <\*>



## MOFLON

- Works on graphs typed by metamodels, specified in MOF



Separate slide set 14b

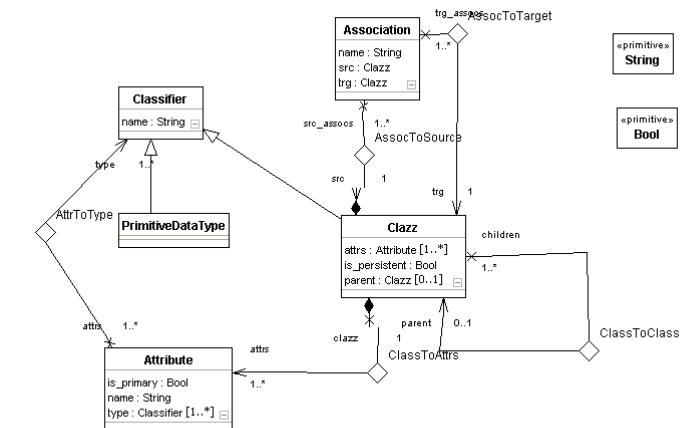
## 14.2 EDGE ADDITION REWRITE SYSTEMS (KANTEN- ERSETZUNGSSYSTEME)

Mapping graphs to other graphs  
Specification of mappings with mapping rules  
Incremental transformation  
Traceability

## 14.3 „SYNCHRONIZING“ MODELS WITH TRIPLE GRAPH GRAMMARS

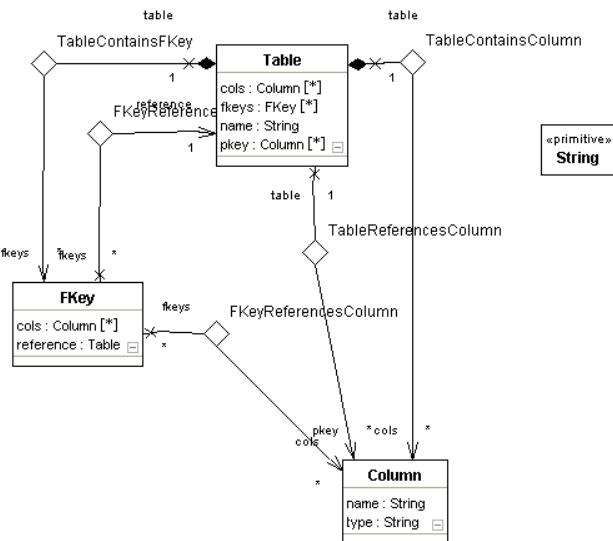
## Triple Graph Grammars – Moflon Example

- Synchronize object-metamodel with a relational schema (ORM)
- Class diagram metamodel (CD)

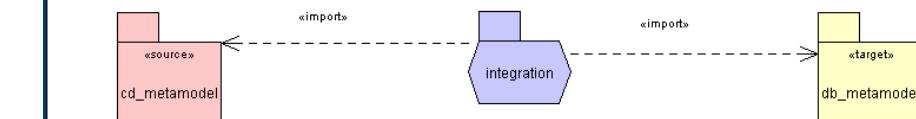


## Triple Graph Grammars – Moflon Example

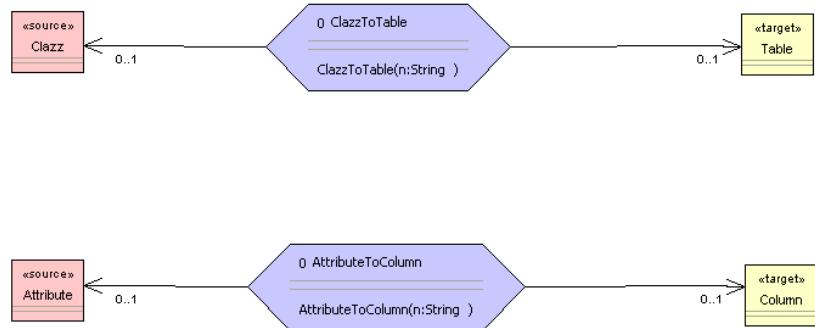
- Relational metamodel (db)



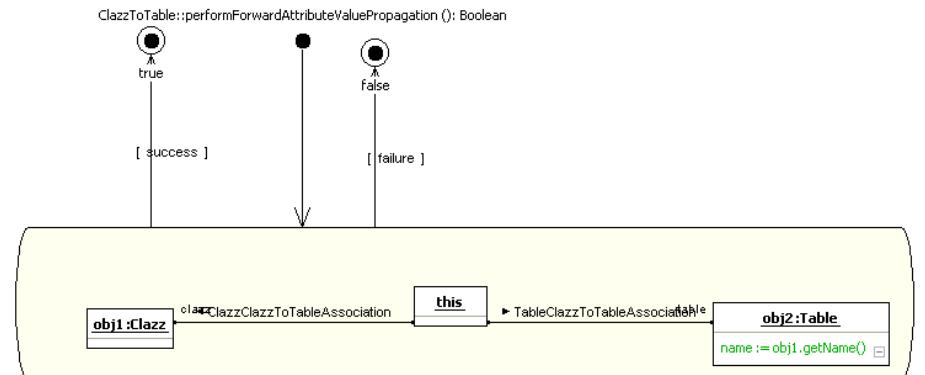
## Triple Graph Grammars – Moflon Example



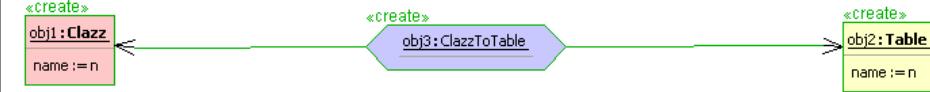
## Triple Graph Grammars – Moflon Example



## Triple Graph Grammars – Moflon Example

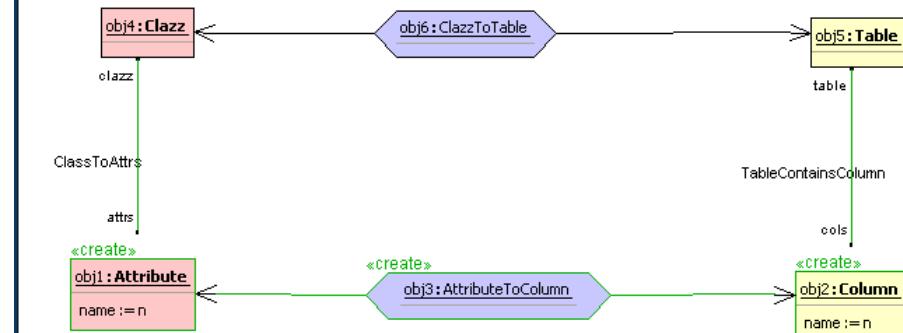


## Triple Graph Grammars – Moflon Example

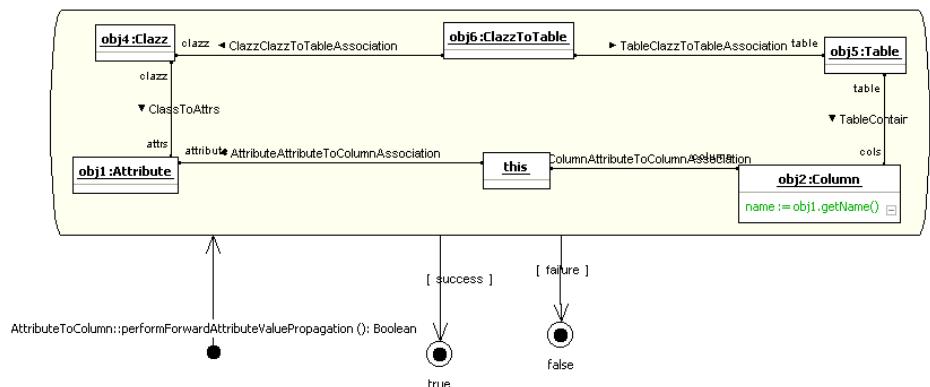


## Triple Graph Grammars – Moflon Example

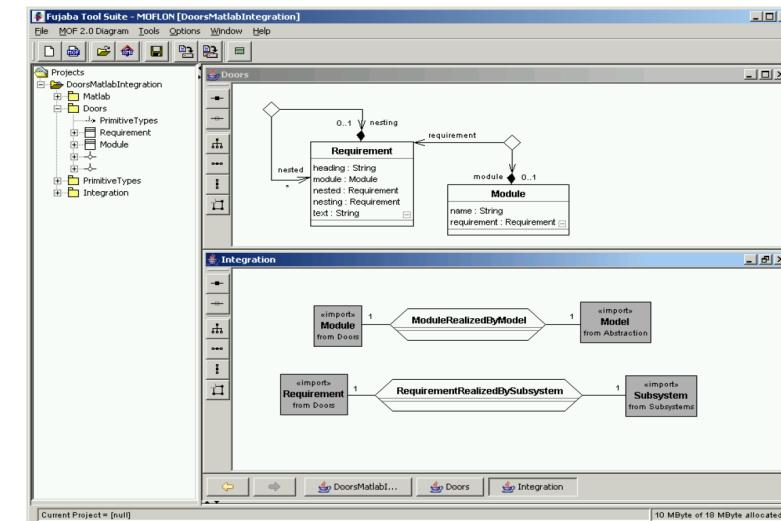
## Triple Graph Grammars – Moflon Example



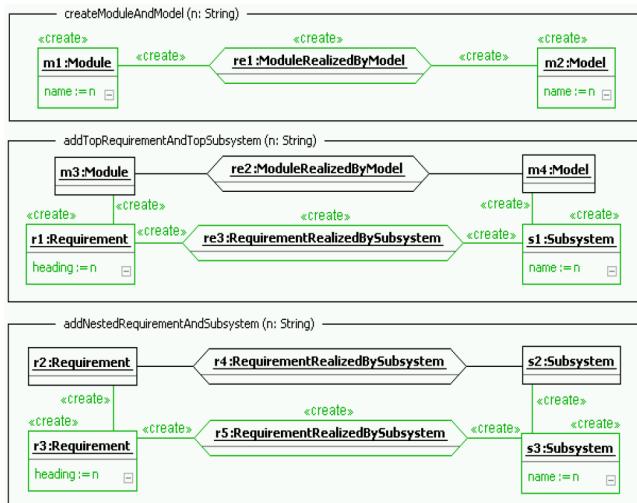
## Triple Graph Grammars – Moflon Example



## TGG Coupling Requirements Specification and Design



## TGG Coupling Requirements Specification and Design



## Other Software Engineering Applications

- Graph Structurings (see later)
- Refactorings (see Course DPF)
- Semantic refinements
- Round-Trip Engineering (RTE)



## The End: What Have We Learned

- Graph rewrite systems are tools to transform graph-based models and graph-based program representations
- TGG enable to bidirectionally map models and synchronize them