### 14b-ST2, 37-SEW **Exhaustive Graph Rewrite** Systems (XGRS) for Model and **Program Transformations**

Prof. Dr. Uwe Aßmann

1) EARS

Softwaretechnologie

2) AGRS

Technische Universität Dresden

3) SGRS

Version 11-0.4, 10.12.11

4) XGRS

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#### **Obligatory Literature**

- Uwe Aßmann. Graph rewrite systems for program optimization. ACM Transactions on Programming Languages and Systems (TOPLAS), 22(4):583-637, June 2000.
  - http://portal.acm.org/citation.cfm?id=363914
- Alexander Christoph. Graph rewrite systems for software design transformations. In M. Aksit, editor, Proceedings of Net Object Days 2002, Erfurt, Germany, October 2002.
- ► Alexander Christoph. GREAT a graph rewriting transformation framework for designs. Electronic Notes in Theoretical Computer Science (ENTCS), 82 (4), April 2003.
- ► Alexander Christoph. Describing horizontal model transformations with graph rewriting rules. In Uwe Aßmann, Mehmet Aksit, and Arend Rensink, editors, MDAFA, volume 3599 of Lecture Notes in Computer Science, pages 93-107. Springer, 2004.
- ▶ Tom Mens. On the Use of Graph Transformations for Model Refactorings. GTTSE 2005, Springer, LNCS 4143
  - http://www.springerlink.com/content/5742246115107431/



#### **Problems with GRS**

With graph rewriting for model and program transformation, there are some problems:

- ► **Termination**: The rules of a GRS G are applied in chaotic order to the manipulated graph. When does G terminate for a start graph?
  - Idea: identify a termination graph which stops the rewriting when completed
- ▶ Non-convergence (indeterminism): when does a GRS deliver a deterministic solution (unique normal form)?
  - Idea: unique normal forms by rule stratification





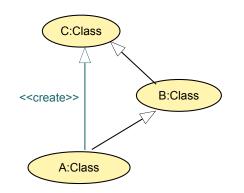
**36.1 EARS** 



#### **Additive Termination**

- ► A **termination subgraph** is a subgraph of the manipulated graph, which is step by step completed
- Conditions in the additive case:
  - nodes of termination (sub-)graph are not added (remain unchanged)
  - its edges are only added
- If the termination graph is complete, the system terminates

#### Transitivising the Inheritance Hierarchy





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[Christoph04]



#### **Example: Collect Subexpressions**

"Find all subexpressions which are reachable from a statement"

ExprsOfStmt(Stmt,Expr) :- Child(Stmt,Expr).

ExprsOfStmt(Stmt,Expr):-Child(Stmt,Expr2), Descendant(Expr2,Expr).

// Descendant is transitive closure of Child

Descendant(Expr1,Expr2):- Child(Expr1,Expr2).

Descendant(Expr1,Expr2) :- Descendant(Expr1,Expr3),

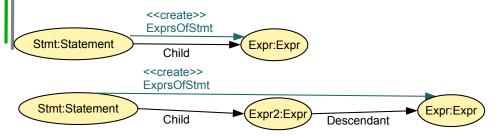
Child(Expr3,Expr2).

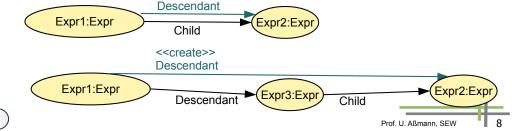
- ► Features:
  - terminating, strong confluent
  - convergent (unique normal form)
  - recursive
- Why do such graph rewrite systems terminate?

#### **EARS CollectExpressions**

<<create>>

Two transitive closures

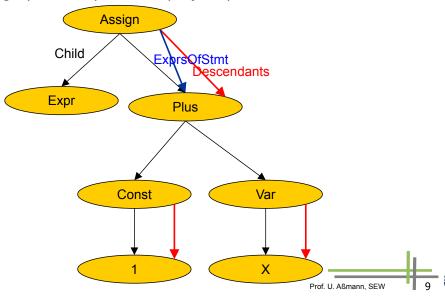




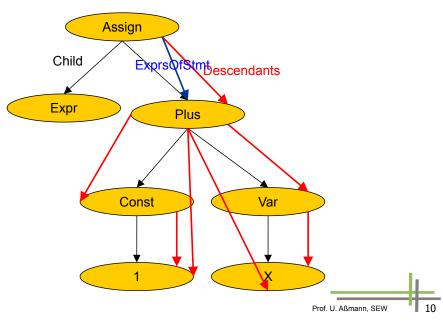


# Execution of "Reachable Subexpressions"

► Answer: ExprsOfStmt and Descendants are termination subgraphs, completed step by step

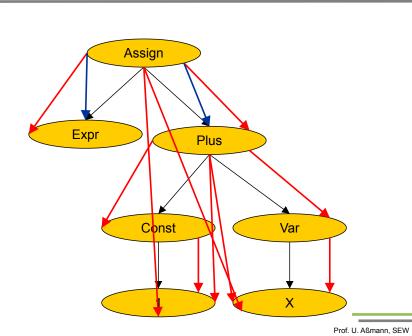


## Execution of "Reachable Subexpressions"

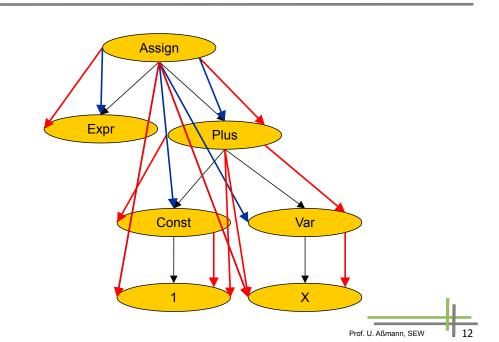


### Execution of "Reachable Subexpressions"

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### Execution of "Reachable Subexpressions"



#### EARS - Simple Edge-Additive GRS

- ► EARS (Edge addition rewrite systems) only add edges to graphs
  - They can be used for the construction of graphs
  - For the building up analysis information about a program or a model
  - For abstract interpretation on an abstract domain represented by a graph
- terminating: noetherian on the finite lattice of subgraphs of the manipulated graph
  - Added edges form the termination subgraph
- strongly confluent: direct derivations can always be interchanged.
- congruent: unique normal form (result)
- ► EARS are equivalent to binary F-Datalog

#### **Data-flow Analysis with EARS**

- Every distributive data flow problem (abstract interpretation problem) on finite-height powerset lattices can be represented by an EARS
  - defined/used-data-flow analysis
  - partial redundancies
  - local analysis and preprocessing:
- ► EARS work for other problems which can be expressed with DATALOG-queries
  - equivalence classes on objects
  - alias analysis
  - program flow analysis



### 36.2 Additive GRS (AGRS)

**Example: Allocation of Register Objects** 

"Allocate a register object for every subexpression of a statement which has a result and link the expression to the statement"

if ExprsOfStmt(Stmt,Expr), HasResult(Expr)

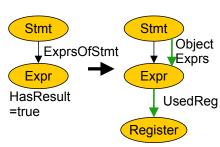
then

ObjectExprs(Stmt,Expr),

RegisterObject := new Register;

UsedReg(Expr,RegisterObject)

► Features: terminating

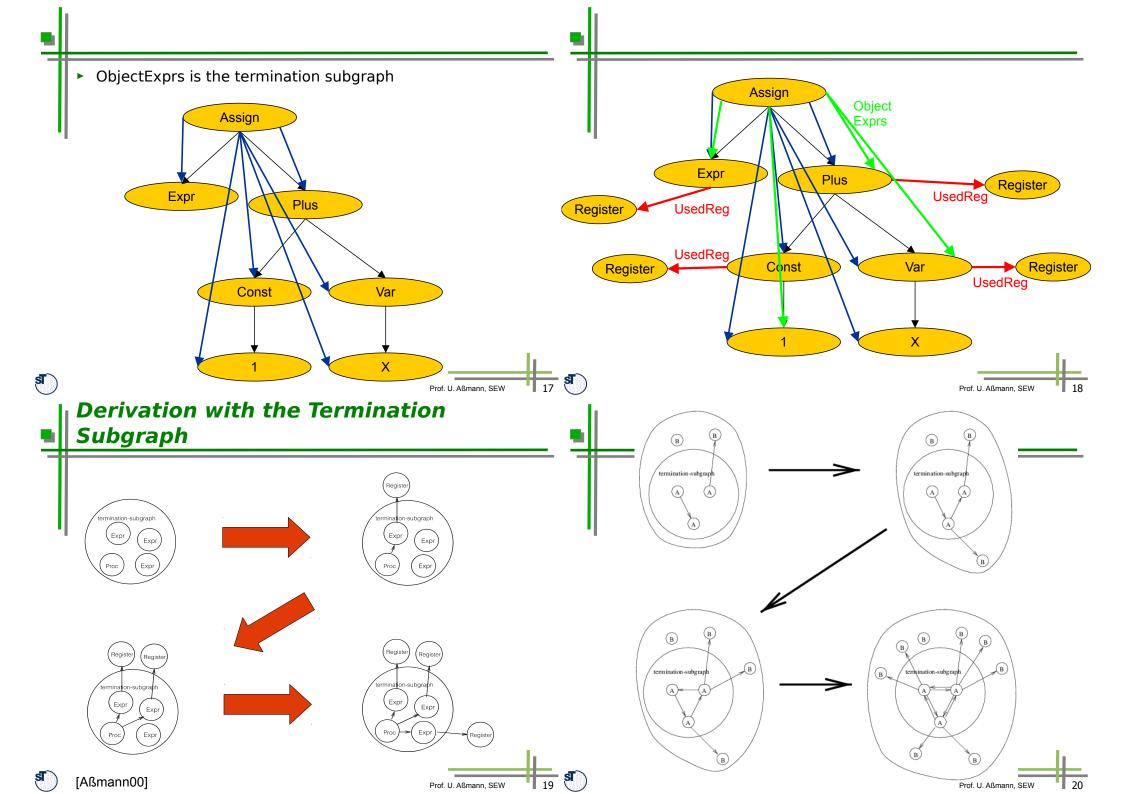








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#### **Edge-accumulative Rules and AGRS**

- ► A GRS is called **edge-accumulative (an AGRS)** if
  - all rules are edge-accumulative and
  - no rule adds nodes to the termination-subgraph nodes of another rule.
- ▶ Edge-accumulative rules are defined on label sets of nodes and edges in rules
- ► This criterion statically decidable

#### The Termination Subgraph of the **Examples**

Collection of subexpressions:

T = ({Stmt,Expr}, {ExprsOfStmt, Descendant})

Allocation of register objects:

T = ({Proc,Expr}, {ObjectExprs})





### 36.3 Subtractive GRS (SGRS)

Conditions in the subtractive case:

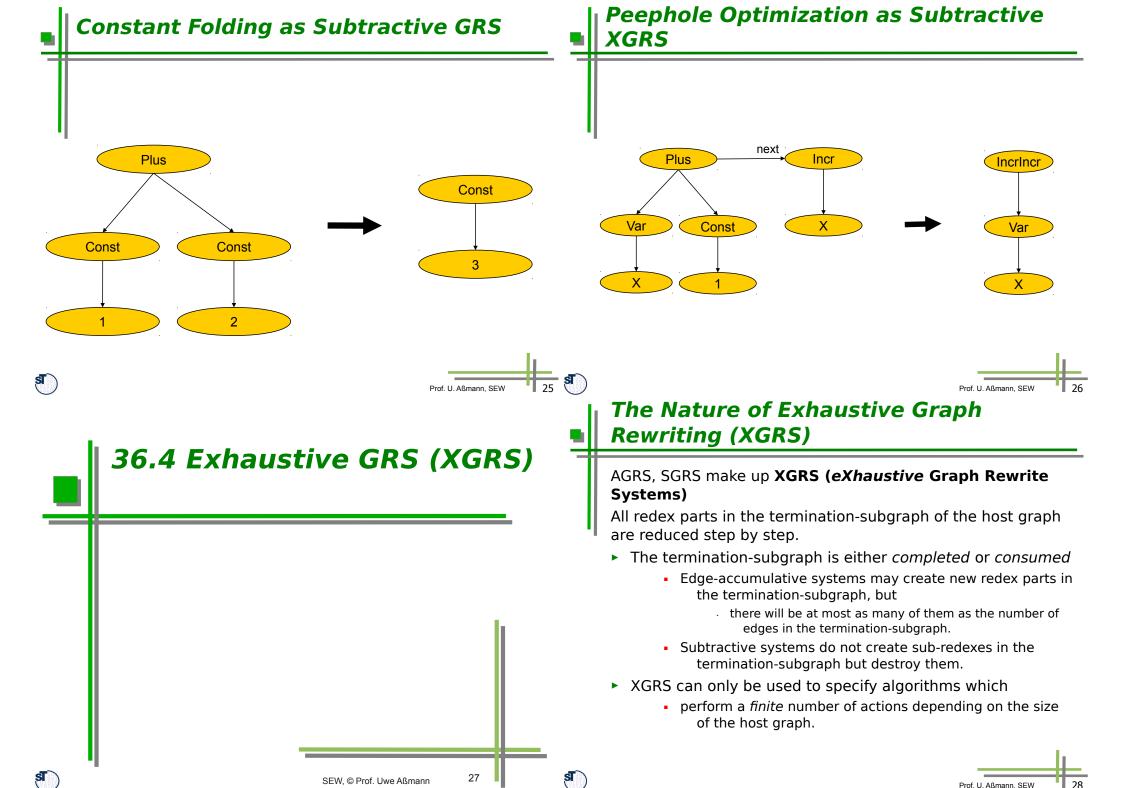
**Subtractive Termination** 

- the nodes of the termination subgraph are not added (remain unchanged)
- its edges are only deleted
- ▶ If the termination subgraph is empty, the system terminates
- Results in:
  - edge-subtractive GRS (ESGRS)
  - subtractive GRS (SGRS)



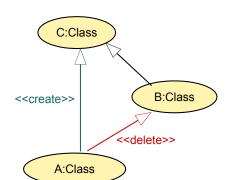
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## All Together Now: Flattening the Inheritance Hierarchy

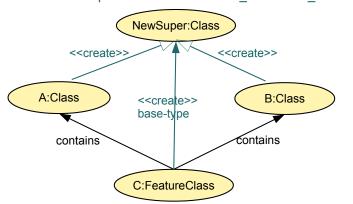
► This rule terminates, due to path contraction





Additive Step 1: Create a new base class for common features; mark this as "base-type"

NewSuper.Name := "<A.name> <B.name> Base"

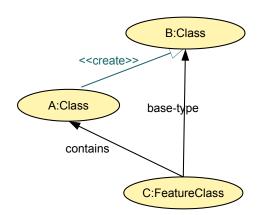


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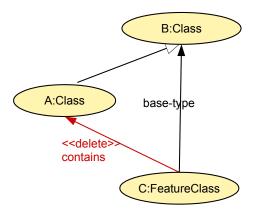
[Christoph04]



 Edge-Additive Step 2: alternate case: a class A has features that should be moved up anyway



Subtractive Step 3: do the real "pull-up" into the superclass



{ forall f in C: move f to B }





#### The End

- Many model and program transformations can be specified by XGRS
- ► Termination criteria build on a *termination subgraph* that is completed or deleted during the transformation



