

51. Model and Program Analysis with Graph Reachability

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Prof. Dr. Uwe Aßmann Softwaretechnologie Technische Universität Dresden Version 12-0.6, 17.01.13 1)Model Mapping

2)EARS for Reachability

3)Regular graph reachability
1)Graph slicing

4)Context-free graph reachability

5)More on the Graph-Logic Isomorphism

6)Implementation in Tools

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Other References

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Tools in an Integrated Development Environment (IDE)

 Model mappings relate different artefacts to enable traceability (reachability) and impact analysis



Reachability analysis (traceability)

Attribute analysis

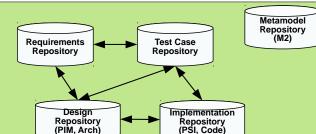








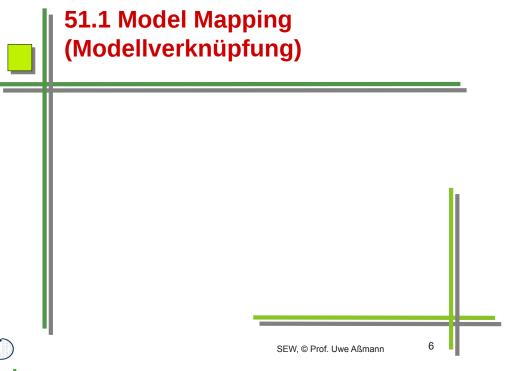






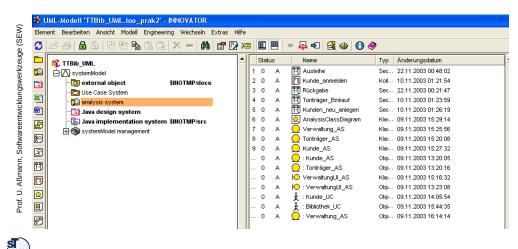
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- Tutorial über ATL "Families2Persones"
- http://www.eclipse.org/m2m/atl/doc/ATLUseCase_Families2Persons. ppt
- ► ATL Zoo von Beispielen
 - http://www.eclipse.org/m2m/atl/atlTransformations
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 - http://www.dcs.kcl.ac.uk/staff/kcl/tcat.pdf
- Implementation in ATL
 - http://www.eclipse.org/m2m/atl/atlTransformations/EquivalenceAttributes
 Associations/EquivalenceAttributesAssociations.pdf

Model Mappings and Model Weavings Model mappings connect models horizontally (on the Domain model for application domain same level) or vertically (crossing levels). Model transformations transform models horizontally or From a model mapping, a simple transformation can Computationally-Independent Model (CIM) Requirements specification Model weavings weave two input models to an output model, based on a crosscut specification Model extensions (model merges, model additions) Platform-Independent Model (CIM) Design specification extend an input model by an extension (often done by hand) Usually, some parts are still hand-written code Model2Text expansion (code generation by template expansion) Weaving Platform-Specific Extension (PSE) Platform Description Model (PDM) Platform Specific Model (PSM) Code addition Handwritten code Platform-Specific Implementation (PSI, Code)



Model Mapping (Modell-Verknüpfung) with MID INNOVATOR

- ► Innovator can be used for requirements models, design models, implementation models, as well as for transformations in between
- How to relate these models systematically?

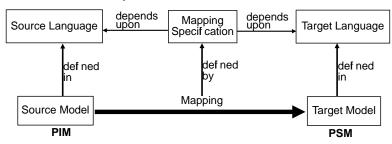


Rpt. from ST-II: Model Mapping, Transformation and Synchronization in the MDA

The MDA architecture derives from a *platform-independent model* (**PIM**) by hand, by rules, by transformations, by metaprograms platform-specific models (PSM)

Model mapping connects systematically all elements of a **source** model to the elements of a target model.

► From the mappings, a translation, transformation, or synchronization can be automatically infered.



Quelle: Kleppe, A., Warmer, J., Bast, W.: MDA Explained - Practice and Promise of the Model Driven Architecture; Addison Wesley 2003 (Draft 25.10.02)

51.1.1 Query-View-Transformations (QVT)

The language of the OMG for model transformations within MDA



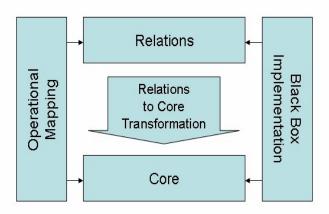


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- We need graph reachability analyzers
 - to create trace graphs for reachability and traceability
 - to create model mappings, model slicings
 - to prepare refactorings, transformers, and optimizers
 - For models: For model refactoring, adaptation and specialization, weaving and composition
 - For code: Portability to new processor types and memory hierarchies
 - For optimization (time, memory, energy consumption)
- However, reachability analyzers are big beasts
 - Current implementation techniques are hard to understand and to a large extent unsystematic
- ► Idea: Use graph-logic isomorphism

OVT Dialects

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QVT relations uses logic expressions on base and derived relations (graph-logic isomorphism)

```
// Transitive Closure in QVT relations,
// Modeled with recursiven relation "transitiverelation"
relation transitiverelation {
 domain node:Node {
  // matching attributes
  name = sameName:
 domain node2:Node {
                          when {
  // node2 must have the
                             // conditions: base relation must exist
  // same name as node
                             baserelation(node,node2) or
  name = sameName:
                             // or a transitive relation to a base relation
                             (transitiverelation(node,neighbor)
 domain node3:Node {
                             and baserelation(neighbor,node2));
  // node3 must also
  // have the same name
                            where { // Aufruf einer Transformation
  name = sameName;
                             makeNodeSound(node);
```



OVT Tools

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Tool			
Eclipse M2M Project	Operational	http://www.eclipse.org/m2m/	
Magic Draw	Operational		
MediniQVT	Relational	http://projects.ikv.de/qvt/wiki	



OCL for Model Search, Query, and Mapping

- OCL is a graph-guery language, similar to EARS and .QL
- ► OCL can be called within QVT scripts
 - Two different DQL are combined within a single language

```
// this is QVT
rule checkNoDoubleFeatureInSuperClasses(name:String) {
  from node: Class (
    node->TransitiveClosure()->collect.().exists(s |
s.name() = name);
  )
  to
    System.out.println("Error: super class has doubly defined feature: "+s.name());
}
```

51.2 Using EARS for Analysis and Mappings of Models and Code

- Graph reachability engines are A-tools answering questions about structure of models and programs
- EARS can be employed for regular graph reachability, context-free graph reachability, slicing, data-flow analysis



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EARS for Model Mapping

QVT Relational is a language for **Edge addition rewrite systems** (**EARS**)

- EARS can be used for model mapping:
 - Transitive closure
 - Regular path reachability
 - Context-free path reachability

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- 1) Specification of the data model (graph schema)
 - Specification of the graph schema with a graph-like DDL (ERD, MOF, GXL, UML or similar):
 - Schema of the program representation: program code as objects and basic relationships. This data, i.e., the start graph, is provided as result of the parser
 - Schema of analysis information (the infered predicates over the program objects) as objects or relationships
- 2) Program analysis (preparing the abstract interpretation)
 - Querying graphs, enlarging graphs
 - Materializing implicit knowledge to explicit knowledge
 - Materializing model mappings
- 3) Abstract Interpretation (program analysis as interpretation)
 - Specifying the transfer functions of an abstract interpretation of the program with graph rewrite rules on the analysis information
- 4) Model and Program transformation (optimization)
 - Transforming the program representation



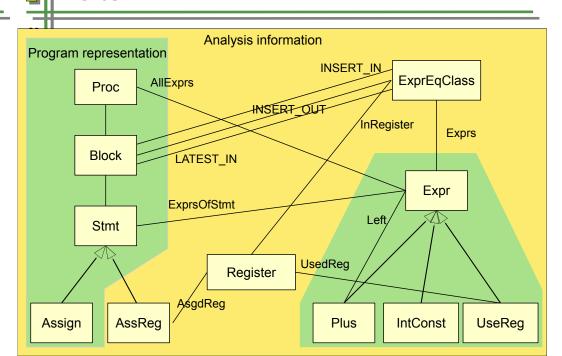
Model Analysis with Graph Reachability

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- Use the graph-logic-isomorphism: Represent everything in a program or a model as directed graphs
 - Program code (control flow, statements, procedures, classes)
 - Model elements (states, transitions, ...)
 - Analysis information (abstract domains, flow info ...)
 - Directed graphs with node and edge types, node attributes, one-edge condition (no multi-graphs)
- Use edge addition rewrite systems (EARS) and other graph reachability specification languages to
 - Query the graphs (on values and patterns)
 - Analyze the graphs (on reachability of nodes)
 - Map the graphs to each other (model mapping)
- ► Later: Use graph rewrite systems (GRS) to construct and augment the graphs, transform the graphs
- Use the graph-logic isomorphism to encode
 - Facts in graphs
 - Logic queries in graph rewrite systems

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A Simple Program (Code) Model (Schema) in MOF/UML





51.2. Simple Reachability: Path Abbreviations in Graph Analysis

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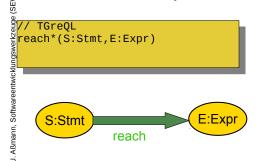
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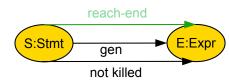
With edge addition rewrite systems

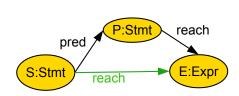
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Transitive Closure

- ► Reachability most often can be reduced to transitive closure
- "Does an Stmt S reach a expression E?"
- Left or right recursion in F-Datalog
- Kleene * in TgreQL
- ► Thick arrow in Fujaba





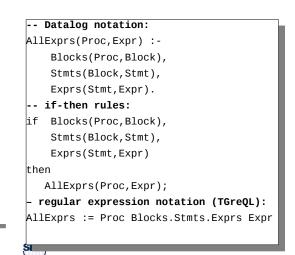


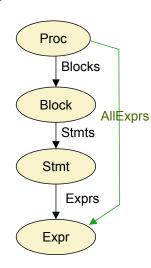
// F-Datalog
reach(S:Stmt,E:Expr) :- gen(S:Stmt,E:Expr), not killed(S:Stmt,E:Expr).
reach(S:Stmt,E:Expr) :- pred(S:Stmt,P), reach(P,E:Expr).

Path Abbreviations

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- ▶ Path abbreviations shorten paths in the manipulated graph.
- They may collect nodes into the neighborhood of other nodes.
- Ex.: Collection of Expressions for a procedure: edge addition



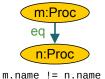


Relating Nodes into Equivalence Classes

- ► Ex.: Computing equivalent nodes
- ► Context-sensitive problem, because m is not in the context of n

```
baserule:
eq(m:Proc,n:Proc) :-
    m.name != n.name.

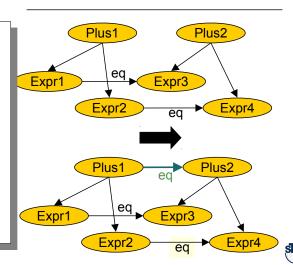
-
If (m:Proc, n:Proc) and m.name !=
    n.name)
    eq(m,n)
}
- TgreQL regular expression:
m:Proc eq n.Proc if
m.name != n.name
```



Ex.: Computing structurally equivalent expressions

IntConst eq IntConst2

baserule:
eq(IntConst1, IntConst2) : IntConst1 ~ IntConst(Value),
 IntConst2 ~ IntConst(Value).
recursive_rule:
eq(Plus1, Plus2) : Plus1 ~ Plus(Type),
 Plus2 ~ Plus(Type),
 Left(Plus1, Expr1),
 Right(Plus1, Expr2),
 Left(Plus2, Expr3),
 Right(Plus2, Expr4).
 eq(Expr1, Expr3),
 eq(Expr2, Expr4).



Data-flow Analysis for Reachability and Traceability

- Data-flow analysis is a specific form of abstract interpretation asking reachability questions, i.e., computing the flow of data through the program, from variable assignments to variable uses
 - Result: the value-flow graph (data-flow graph)
- **Examples of reachability problems:**
- ► AllSuperClasses: find out for a class transitively all superclasses
- ► AllEnclosingScopes: find out for a scope all enclosing scopes
- Reaching Definitions Analysis: Which Definitions (Assignments) of a variable can reach which statement?
- ► Live Variable Analysis: At which statement is a variable live, i.e., will further be used?
- Busy Expression Analysis: Which expression will be used on all outgoing paths?
 - Central part: 1 recursive system

51.3. Data-Flow Analysis as Graph Reachability

with edge additions

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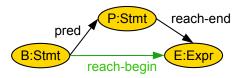
Reaching Definition Analysis

Reaching Definitions Analysis:

- Which Assigments of a variable can reach which using statement?
- Which variable definitions reach which expression?
- Graph rewrite rules implement an abstract interpreter
 - On instructions or on blocks of instructions
 - Flow information is expressed with edges of relations "reach-*"
- Recursive system (via edge reachbegin)
 - B reach-end E == E reaches end of block B







reach-end(B,E) :- gen(B,E).
reach-end(B,E) :- reach-begin(B,E), not killed(B,E).
reach-begin(B,E) :-pred(B,P), reach-end(P,E).

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- **Code motion** is an essential transformation to speed up the generated code. However, it is a complex transformation:
 - Discovering loop-invariant expressions by data-flow analysis
 - Moving loop-invariant expressions out of loops upward
 - Code motion needs complex data-flow analysis
- ▶ Busy Code Motion (BCM) moves expressions as upward (early) as possible
- Lazy Code Motion (LCM)
 - Moving expressions out of loops to the front of the loop, upward, but carefully:
 - Moving expressions to an optimal place so that register lifetimes are shorter and not too long (optimally early)
 - LCM analysis computes this optimal early place of an expression [Knoop/Steffen]
 - · Analyze an optimally early place for the placement of an expression
 - About 6 equation systems similar to reaching-definitions
 - Every equation system is an EARS

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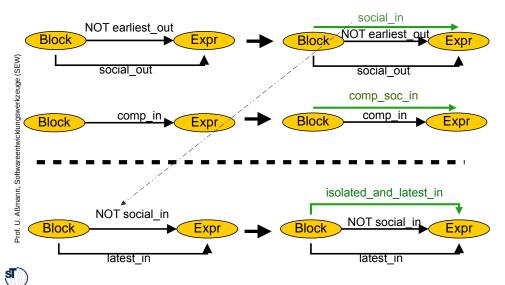
51.3 Regular Graph Reachability





Excerpt from LCM Analysis with Overlaps

Compute an optimally early block for an expression (out of a loop)



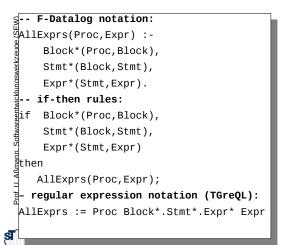


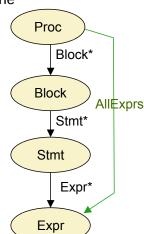
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Regular Graph Reachability

- If the query can be expressed as a regular expression, the query is a regular graph reachability problem
 - Kleene star is used as transitive closure operator
- ► TqreQL and Fujaba are languages offering Kleene *







51.3.1 Static Slicing: Single-Source-Multiple-Target Regular Reachability

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[Weiser] [Tip]

- ► A **static slice** is the region of a program or model reached from *one* source node by a regular reachability query
- ► A **forward slice** is a region in forward direction of the program
 - The uses of a variable
 - The callees of a call
 - · The uses of a type
- ▶ A **backward slice** is a region in backward direction of the program
 - The assignments which can influence the value of a variable
 - The callers of a method
 - The type of a variable
- ► A static slice introduces path abbreviations from one entity to a region
- Slicing can map arbitrary entities in programs and models to other entities, based on a regular graph expression

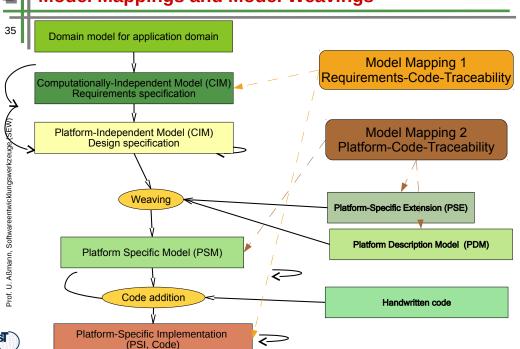
Traceability between Models

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- ► Data-flow analysis (graph reachability, slicing) can be done
 - intraprocedurally
 - Interprocedurally (program-wide)
 - intermodel: then it creates trace relations
 - interspecification: between requirements models, design models, and code models
 - Inter-MDA
- ► Traceability is intermodel slicing and graph reachability
- ► A model mapping is an intermodel trace graph

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Application of Traceability: Model Mappings and Model Weavings



51.3.2 Context-Free Graph Reachability



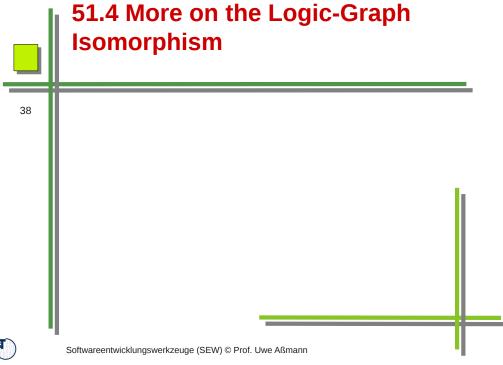
- F-Datalog and EARS can describe other recursions than regular ones (linear recursions)
 - Context-free recursions
 - Cross-recursions
- ► Then, we speak of context-free graph reachability
 - A context-free language describes graph reachability
- Application: interprocedural, whole-program analysis (see separate optional chapter)
 - Interprocedural IDFS framework (Reps)



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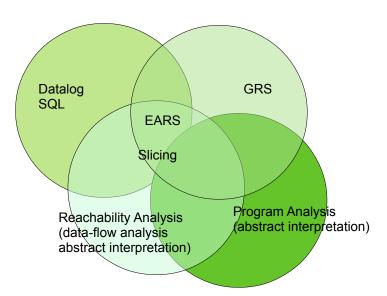
- Reachability Analysis is a simple form of abstract interpretation
 - Slicing is a Single-Source-Multiple-Target reachability analysis
- Every abstract interpretation where a mapping of the abstract domains to graphs can be found.
 - monotone and distributive data-flow analysis
 - control flow analysis
 - SSA construction
 - Interprocedural IDFS framework (Reps)



The Common Core of Logic, Graph Rewriting and Program Analysis

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 Graph rewriting, DATALOG and data-flow analysis have a common core: EARS







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- Abstract interpretation (Data-flow analysis), DATALOG and graph rewrite systems have a common kernel: EARS
 - As DATALOG, graph rewrite systems can be used to query the graph.
- Contrary to DATALOG graph rewrite systems materialize their results instantly.
 - Graph rewriting is restricted to binary predicates and always yields all solutions.
- Graph rewriting can do transformation, i.e. is much more powerful than DATALOG.
 - Graph rewriting enables a uniform view of the entire optimization process
 - There is no methodology on how to specify general abstract interpretations with graph rewrite systems
 - In interprocedural analysis, instead of chaotic iteration special evaluation strategies must be used [Reps95] [Knoop92].
 - Currently strategies have to be modeled in the rewrite specifications explicitly.

51.5 Implementation in Tools





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- Uniform Specification of Analysis and Transformation
 - If the program analysis (including abstract interpretation) is specified with GRS
 - It can be unified with program transformation





- ► Tool OPTIMIX uses the "Order algorithm" scheme [Aßmann00]
 - Variant of nested loop join
 - Easy to generate into code of a programming language
 - Works effectively on very sparse directed graphs
 - Sometimes fixpoint evaluations can be avoided
 - Use of index structures possible
 - Linear bitvector union operations can be used
- ► F-DATALOG optimization techniques can be employed
 - Bottom-up evaluation is normal, as in F-Datalog
 - Top-down evaluation as in Prolog possible, with resolution
 - semi-naive evaluation
 - index structures
 - magic set transformation
 - transitive closure optimizations

Fujaba and MOFLON graph rewrite systems

- TGG for Model Mapping
- QVT Relational is very similar to TGG
- See chapter MOFLON and course ST-II
- AGG graph rewrite system (From Berlin)
- VIATRA2 graph rewrite system
- Program Analysis Generators
 - PAG (Alt, Martin)
 - Sharlit (Tijang)
 - MetaFrame with modal logic (Knoop, Steffen)
 - Slicing-Tools (Reps, Field/Tip, Kamkar)



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- Graph rewrite rule: rule (left, right hand side) to match left-hand side in the graph and to transform it to the right-hand side
- Graph rewrite system: set of graph rewrite rules
- Start graph (axiom): input graph to rewriting
- Graph rewrite problem: a graph rewrite system applied to a start graph
- Manipulated graph (host graph): graph which is rewritten in graph rewrite problem
- ▶ Redex: (reducible expression) application place of a rule in the manipulated graph
- Derivation: a sequence of rewrite steps on the manipulated graph, starting from the start graph and ending in the normal form
- Normal form: result graph of rewriting; manipulated graphs without further redex
- Unique normal form: unique result of a rewrite system, applied to one start graph
- Terminating GRS: rewrite system that stops after finite number of rewrites
- Confluent GRS: two derivations always can be commuted, resp. joined together to one result
- Convergent GRS: rewrite system that always yields unique results (terminating and confluent)





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- Explain program slicing
- Why is regular graph reachability "regular"?
- How do you create a model mapping with regular graph reachability?

Explain a typical data-flow analysis

