

3. Modelling Dynamic Behavior with Petri Nets

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- 1) Basics
 - 1) Elementary Nets
 - 2) Colored Petri Nets
- 2) Patterns in Petri Nets
- 3) Refactorings
- 4) Composability of Colored Petri Nets
- 5) Parallel Composition with CPN
- 6) Application to modelling

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Literature

- 3
- ▶ K. Jensen: Colored Petri Nets. Lecture Slides <http://www.daimi.aau.de/~kjensen> Many other links and informations, too
 - www.daimi.aau.dk/CPnets the home page of CPN. Contains lots of example specifications. Very recommended
 - ▶ K. Jensen, Colored Petri Nets. Vol. I-III. Springer, 1992-96. Landmark book series on CPN.
 - ▶ T. Murata. Petri Nets: properties, analysis, applications. IEEE volume 77, No 4, 1989.
 - ▶ W. Reisig. Elements of Distributed Algorithms – Modelling and Analysis with Petri Nets. Springer. 1998.
 - ▶ W. Reisig, G. Rozenberg: Lectures on Petri Nets I+II, Lecture Notes in Computer Science, 1491+1492, Springer.
 - ▶ J. Peterson. Petri Nets. ACM Computing Surveys, Vol 9, No 3, Sept 1977
 - ▶ http://www.daimi.au.dk/CPnets/intro/example_indu.html

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Obligatory Readings

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- ▶ Balzert 2.17
- ▶ Or Ghezzi Chap 5
- ▶ or (not enough in Pfleeger):
- ▶ W.M.P. van der Aalst and A.H.M. ter Hofstede. Verification of workflow task structures: A petri-net-based approach. Information Systems, 25(1): 43-69, 2000.
- ▶ Kurt Jensen, Lars Michael Kristensen and Lisa Wells. Coloured Petri Nets and CPN Tools for Modelling and Validation of Concurrent Systems. Software Tools for Technology Transfer (STTT). Vol. 9, Number 3-4, pp. 213-254, 2007.
- ▶ J. B. Jörgensen. Colored Petri Nets in UML-based Software Development – Designing Middleware for Pervasive Healthcare. www.pervasive.dk/publications/files/CPN02.pdf
- ▶ Web portal “Petri Net World” <http://www.informatik.uni-hamburg.de/TGI/PetriNets/>

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Relationship of PN and other Behavioral Models

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- ▶ P.D. Bruza, Th. P. van der Weide. The Semantics of Data-Flow Diagrams. Int. Conf. on the Management of Data. 1989
 - <http://citeseer.ist.psu.edu/viewdoc/summary?doi=10.1.1.40.9398>
- ▶ E.E.Roubtsova, M. Aksit. Extension of Petri Nets by Aspects to Apply the Model Driven Architecture Approach. University of Twente, Enschede, the Netherlands
- ▶ Other courses at TU Dresden:
 - Entwurf und Analyse mit Petri-Netzen
 - Lehrstuhl Alg. u. log. Grundlagen d. Informatik
 - Dr. rer. nat. W. Nauber
 - <http://wwwtcs.inf.tu-dresden.de/~nauber/eapn10add.html>

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Goals

- ▶ Understand untyped and Colored Petri nets (CPN)
- ▶ Understand that CPN are a verifiable and automated technology for safety-critical systems
- ▶ PN have subclasses corresponding to finite automata and data-flow graphs
- ▶ PN can be refined, then reducible graphs result

The Initial Problem

- ▶ You work for PowerPlant Inc. Your boss comes in and says:

Our government wants a new EPR reactor, similarly, in the way Finland has it. How can we produce a verified control software?
We need a good modelling language. Assembler would be too bad...

UML does not work...

How do we produce software for safety-critical systems?

Interesting Projects with Safety-Critical, Parallel Embedded Software

- ▶ Arial
 - The WITAS UAV unmanned autonomously flying helicopter from Linköping
http://www.ida.liu.se/~marwz/papers/ICAPS06_System_Demo.pdf
- ▶ Automotive
 - Prometheus: driving in car queues on the motorway
<http://www.springerlink.com/content/j06n312r36805683/>
- ▶ Trains
 - www.railcab.de Autonomous rail cabs
 - www.cargocab.de Autonomous cargo metro
http://www.cargocab.de/files/cargocab_presse/2005/2005_01_12%20kruse.pdf
 - <http://www.rubin-nuernberg.de/> Autonomous mixed metro

Application Areas of Petri Nets

- ▶ Model introduced by C.A. Petri in 1962.
 - Ph.D. Thesis: "Communication with Automata".
 - Over many years developed within GMD (now Fraunhofer, FhG)
 - PNs describe explicitly and graphically: Conflict/non-deterministic choice, concurrency
- ▶ Reliable software (quality-aware software)
 - PetriNets can be checked on deadlocks, liveness, fairness, bounded resources
- ▶ Safety-critical software that require proofs
 - Control software in embedded systems or power plants
- ▶ User interface software
 - Users and system can be modeled as separate components
- ▶ Hardware synthesis
 - Software/Hardware co-design

Application Area I: Behavior Specifications in UML

- 9 ▶ Instead of describing the behavior of a class with a statechart, a CPN can be used
- ▶ CPN have several advantages:
 - They model parallel systems naturally
 - They are compact and modular, can be reducible
 - They lend themselves to aspect-oriented composition, in particular of parallel protocols
 - They can be used to generate code, also for complete applications
 - UML statecharts, data flow diagrams, and activity diagrams are special instances of CPN
- ▶ Informal: for CPN, the following features can be proven
 - Liveness: All parts of the net do never get into a dead lock, i.e., can always proceed
 - Fairness: all parts of the net are equally "loaded" with activity
 - K-boundedness: the data that flows through the net is bound by a threshold
 - Deadlock-freeness: the net does not stop (deadlock)



Application Area II: Contract checking (Protocol Checking) for Components

- 10 ▶ Petri Nets describe behavior of components (dynamic semantics)
 - They can be used to check whether components fit to each other
- ▶ Problem: General fit of components is undecidable
 - The protocol of a component must be described with a decidable language
 - Due to complexity, context-free or -sensitive protocol languages are required
- ▶ Algorithm:
 - Describe the behavior of two components with two CPN
 - Link their ports
 - Check on *liveness* of the unified CPN
 - If the unified net is not live, components will not fit to each other...
- ▶ Liveness and fairness are very important criteria in safety-critical systems



3.1 Basics of PN

Petri Net Classes

- Predicate/Transition Nets: simple tokens, no hierarchy.
- Place-Transition Nets: multiple tokens
- High Level Nets: structured tokens, hierarchy
- There are many other variants, e.g., with timing constraints

Language Levels

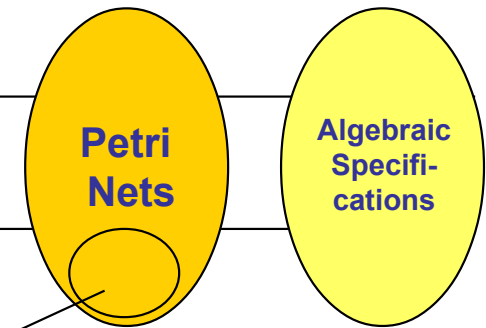
- 12 ▶ PN extend finite automata with indeterminism
 - Asynchronous execution model (partial ordering)

CH-0 computable

CH-1 context sensitive

CH-2 context free

CH-3 regular

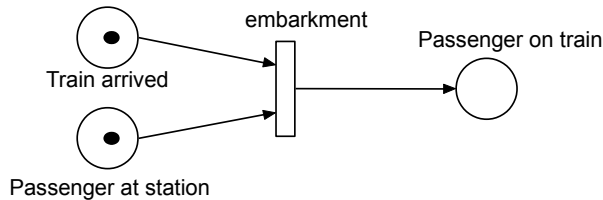


Finite state machines are PN with finite reachability graph



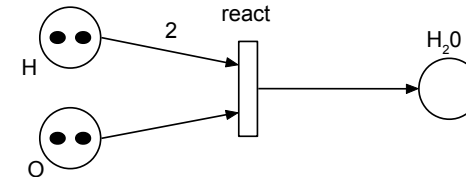
Elementary Nets: Predicate/Transition Nets

- 13
- ▶ A **Petri Net (PN)** is a directed, bipartite graph over two kinds of *nodes*, namely *places* (circles) and *transitions* (bars or boxes)
 - ▶ An *elementary PN* is with boolean tokens, i.e., one token per place (bound of place = 1)
 - aka basic, predicate/transition nets (PTN), condition/Event nets
 - The presence of a token in a place means that the condition or predicate is true
 - The *firing* of a transition means that from the input predicates the output predicates are concluded
 - Thus elementary PN can model simple forms of logic



Integer Place/Transitions-Nets

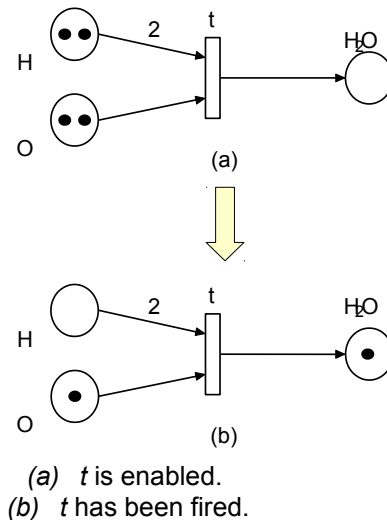
- 14
- ▶ An *integer PN* is a directed, weighted, bipartite graph over places and transitions with *integer* tokens, i.e., places may contain several tokens, and a *capacity* (*bound* = k)
 - k tokens in a place indicate that k data items are available
 - $M(p)$ is the number of tokens in place p
 - ▶ A *marking* assigns to each place a nonnegative integer
 - A marking is denoted by M , an m -vector where m is the number of places.
 - A PN has a *initial marking*, M_0 .
 - ▶ Arcs have *cardinalities* (*weights*) to show how many tokens they transfer



Here: initial marking $M_0(2,2,0)$

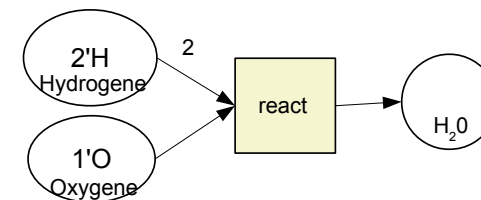
Formal Transition Enabling and Firing

- 15
- In a PN a state is changed according to the following *transitions firing rule*:
- ▶ A transition t is *enabled* if
 - each input place p of t is marked with at least $w(p,t)$ tokens, where $w(p,t)$ is the weight of the arc from p to t
 - The output place can be filled
 - ▶ An enabled transition may or may not fire.
 - ▶ A *firing* of an enabled transition removes $w(p,t)$ tokens from each input place p to t , and adds $w(t,p)$ tokens to each output place p of t , where $w(t,p)$ is the weight of the arc from t to p .



High-Level Nets

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- ▶ A *high-level PN* (*colored PN*) allows for *typed* places and arcs
 - For types, any DDL can be used (e.g., UML-CD)
 - ▶ High-level nets are modular
 - Places and transitions can be refined
 - A Colored Petri Net is a reducible graph
 - ▶ The upper layers of a reducible CPN are called *channel agency nets*
 - Places are interpreted as channels between components



3.1.1 Elementary Nets (Predicate/Transition Nets)

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Meaning of Places and Transitions in Elementary Nets

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- ▶ Predicate/Transition (Condition/Event-, State/Transition) Nets:
 - Places represent conditions, states, or predicates
 - Transitions represent the firing of events:
 - if a transition has one input place, the event fires immediately if a token arrives in that place
 - If a transition has several input places, the event fires when all input places have tokens
- ▶ A transition has *input* and *output* places (pre- and postconditions)
 - The presence of a token in a place is interpreted as the condition is true

Formal Definition of a Place/Transition Net

▶ A PN is a 5-tuple, $P = (P, T, F, W, M_0)$ with

$$P = \{p_1, p_2, \dots, p_m\}$$

is a finite set of places,

$$T = \{t_1, t_2, \dots, t_m\}$$

is a finite set of transitions,

$$F \subseteq (P \times T) \cup (T \times P)$$

is a set of arcs (flow relation),

$$W : F \rightarrow \{1, 2, 3, \dots\}$$

is a weight function,

$$M_0 : P \rightarrow \{0, 1, 2, 3, \dots\}$$

is the initial marking, (if $\text{img}(P) = \{0, 1\}$, we have an elementary net, otherwise an integer net)

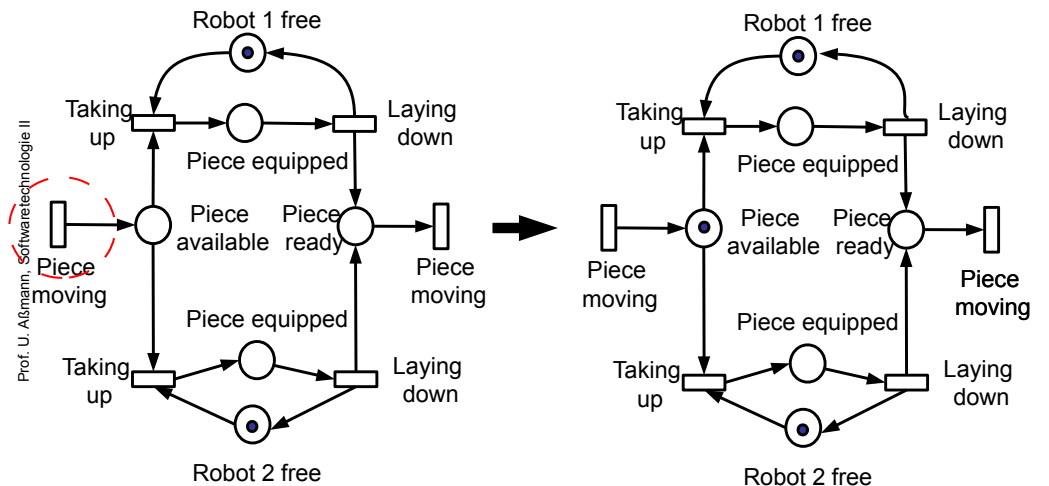
$$P \cap T = \emptyset, P \cup T \neq \emptyset$$

A PN structure $N = (P, T, W)$ without any specific initial marking is denoted N

A PN with the given initial marking is denoted by (N, M_0)

Example of 2 Robots as Predicate/Transition Net

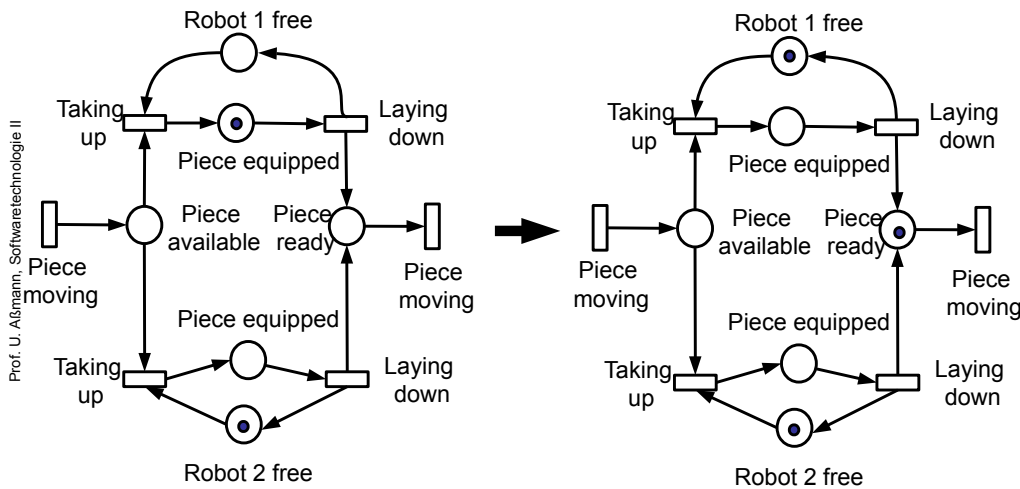
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Example of 2 Robots as Predicate/Transition Net

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- Places represent predicates; tokens show validity



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3.1.2 Special Nets

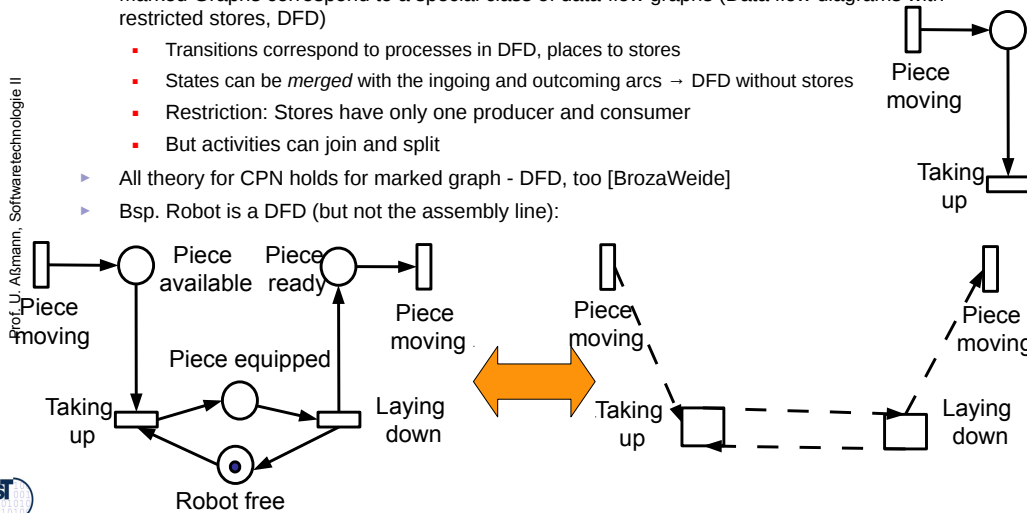
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Marked Graphs (MG)

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- A **Marked Graph (MG)** is an PN such each place is the input to only one transition and the output of only one transition. MG provide *deterministic parallelism without confusion*
 - Then the places can be abstracted (identified with one flow edge)
 - Transitions may split and join, however
- Marked Graphs correspond to a special class of data-flow graphs (Data flow diagrams with restricted stores, DFD)
 - Transitions correspond to processes in DFD, places to stores
 - States can be *merged* with the ingoing and outgoing arcs → DFD without stores
 - Restriction: Stores have only one producer and consumer
 - But activities can join and split
- All theory for CPN holds for marked graph - DFD, too [BrozaWeide]
- Bsp. Robot is a DFD (but not the assembly line):



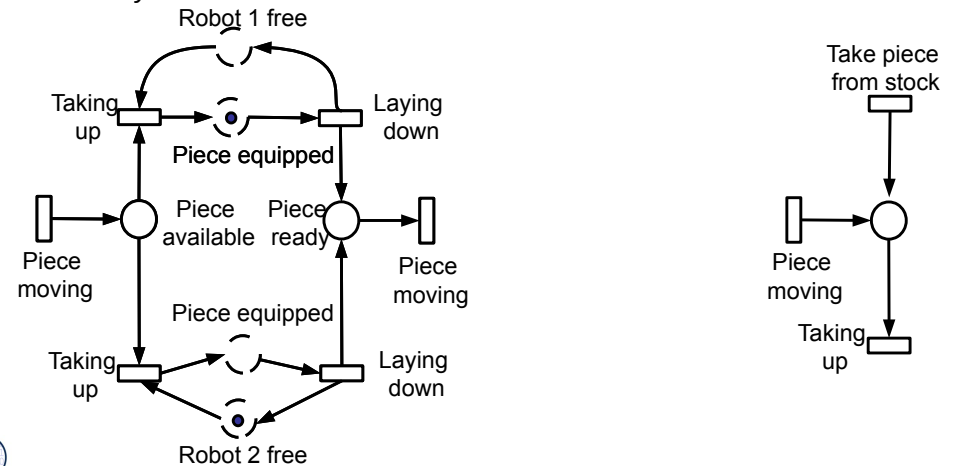
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More General Data-Flow Diagrams

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- General DFD without restriction can be modeled by PN, too. Then, places cannot be abstracted; they correspond to stores with 2 feeding or consuming processes
- Example: the full robot has places with 2 ingoing or outgoing edges, they cannot be abstracted

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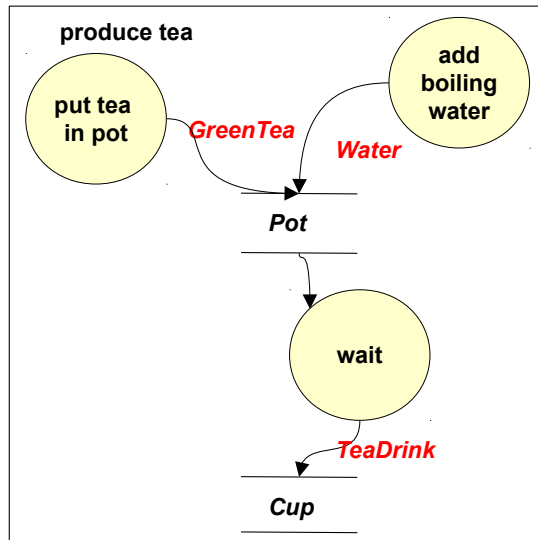


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For DFD, Many Notations Exist

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- ▶ Notation from Structured Analysis [Balzert]



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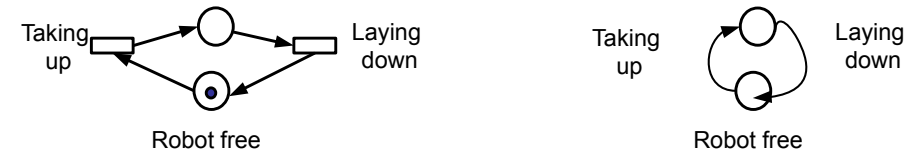


State Machines are PN with Cardinality Restrictions

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- ▶ A *Finite State Machine* PN is an elementary PN such that each transition has only one input and one output place
 - Then, it is equivalent to a finite automaton or a *statechart*
 - From every class-statechart that specifies the behavior of a class, a State Machine can be produced easily
 - Flattening the nested states
 - Transitions correspond to transitions in statecharts, states to states
 - Transitions can be *merged* with the ingoing and outgoing arcs
 - In a FSM there is only one token
- ▶ All theory for CPN holds for Statecharts, too
- ▶ Ex. Robot is an FSM (but not with incoming data flow):

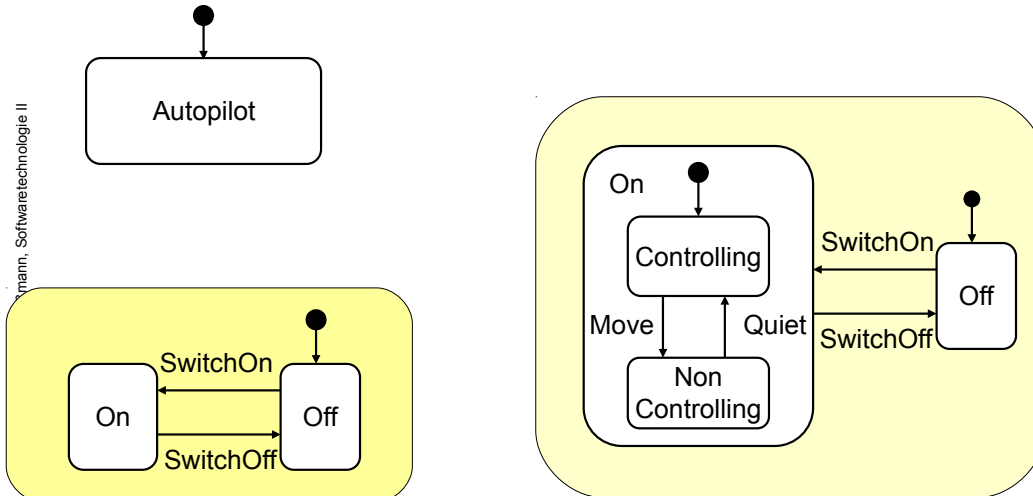
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Hierarchical StateCharts from UML

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- ▶ States can be nested in StateCharts
- ▶ This corresponds to StateMachine-PN, in which states can be refined and nested



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3.1.2 Colored Petri Nets as Example of High Level Nets

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Modularity, Refinement,
Reuse
Preparing "reducible graphs"

Colored Petri Nets, CPN

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- ▶ Colored (Typed) Petri Nets (CPN) refine Petri nets:
 - Tokens are typed (colored)
 - Types are described by data structure language, such as Java, ML, UML class diagrams
 - but may also be data dictionaries, grammars
 - Concept of time can be added
 - ▶ Full tool support
 - Fully automated code generation in Java and ML (in contrast to UML), e.g., DesignCPN of Aarhus University <http://www.daimi.aau.dk>
 - Prover proofs features about the PN
 - Net simulator allows for debugging
 - ▶ Much better for safety-critical systems than UML, because proofs can be done

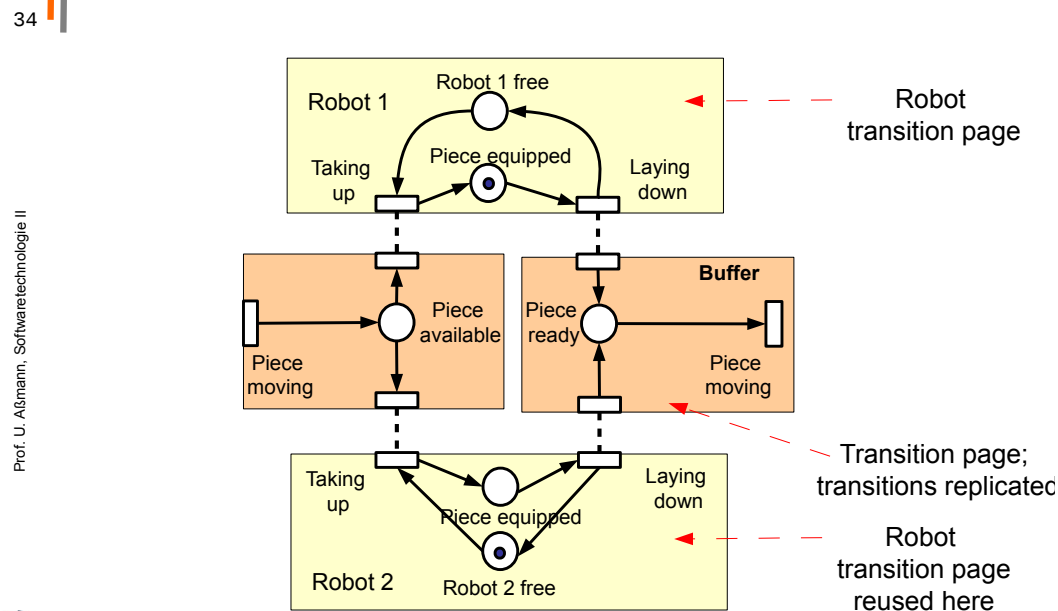
Annotations in CPN

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- ▶ Places are annotated by
 - Token types
 - (STRING x STRING)
 - Markings of objects and the cardinality in which they occur:
 - 2' ("Uwe", "Assmann")
 - ▶ Edges are annotated by
 - Type variables which are unified by unification against the token objects
 - (X, Y)
 - Guards
 - [X == 10]
 - if-then-else statements
 - if X < 20 then Y := 4 else Y := 7
 - switch statements
 - boolean functions that test conditions

CPN are Modular

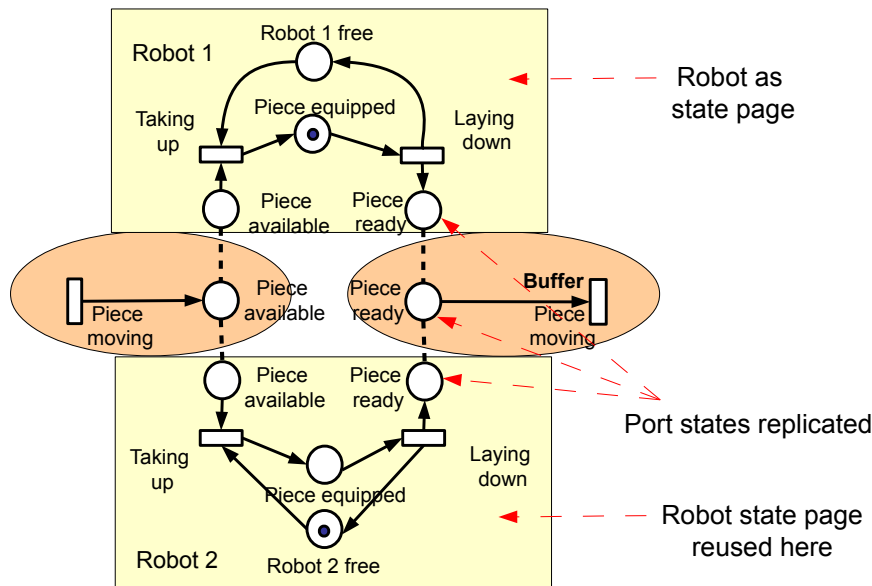
- 33
- ▶ A subnet is called a *page (module)*
 - Every page has ports which mark in- and out-going transitions (into a place) or in- and outgoing places (into a transition)
 - ▶ *Transition page*: interface contains transitions (transition ports)
 - ▶ *Place page (state page)*: interface contains place (place ports)
 - ▶ *Net class*: a named page that is a kind of "template" or "class"
 - It can be instantiated to a net "object"
 - ▶ Reuse of pages and templates possible
 - Libraries of CPN "procedures" possible

Robots with Transition Pages, Coupled by Transition Ports



Robots with Place (State) Pages, Coupled by Replicated State Ports

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CPN are Hierarchical

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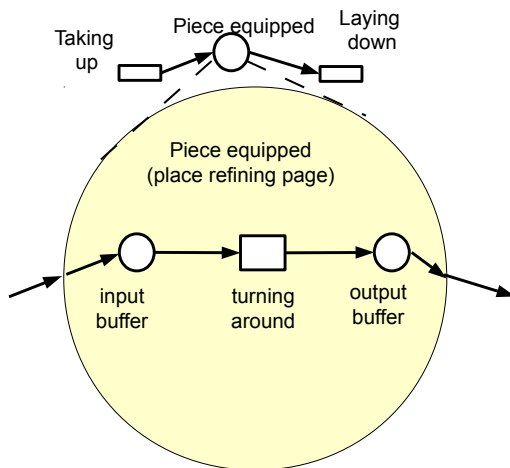
- ▶ Places and transitions may be hierarchically **refined**
 - Two pointwise refinement operations:
 - Replace a transition with a transition page
 - Replace a state with a state page
 - Refinement condition: Retain the embedding (embedding edges)
- ▶ CPN can be arranged as hierarchical graphs (reducible graphs, see later)
 - Large specifications possible, overview is still good
 - Subnet stemming from refinements are also place or transition pages

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Point-wise Refinement Example

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- ▶ Pointwise refinement:
 - *Transition refining page*: refines a transition, transition ports
 - *Place refining page (state refining page)*: refines a place, place ports



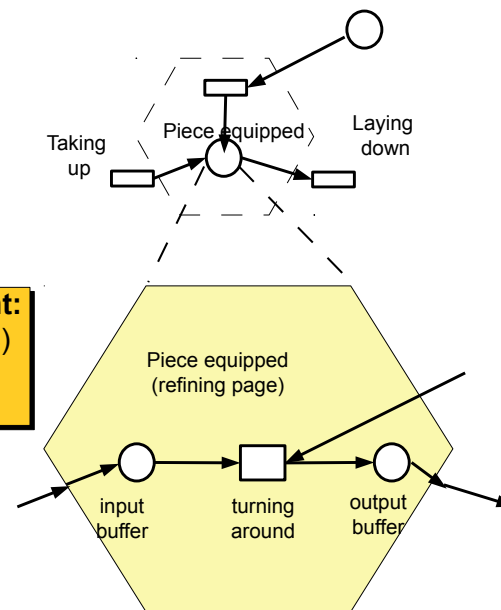
Law of syntactic refinement: The graph interface (attached edges) of a refined node must be retained by the refining page.

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Region (Hyperedge) Refinement Example

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- ▶ Hyperedges and regions in PN can be refined



Law of syntactic region refinement: The graph interface (attached edges) of a refined region must be retained by the refining region.

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Industrial Applications of CPN

- ▶ Large systems are constructed as reducible specifications
- ▶ ..have 10-100 pages, up to 1000 transitions, 100 token types
- ▶ Example: ISDN Protocol specification
 - Some page templates have more than 100 uses
 - Corresponds to millions of places and transitions in the expanded, non-hierarchical net
 - Can be done in several person weeks



Modelling of Parallelism and Synchronization

Petri Nets have a real advantage when parallel processes and synchronization must be modelled
 Many concepts can be expressed as *PN patterns*

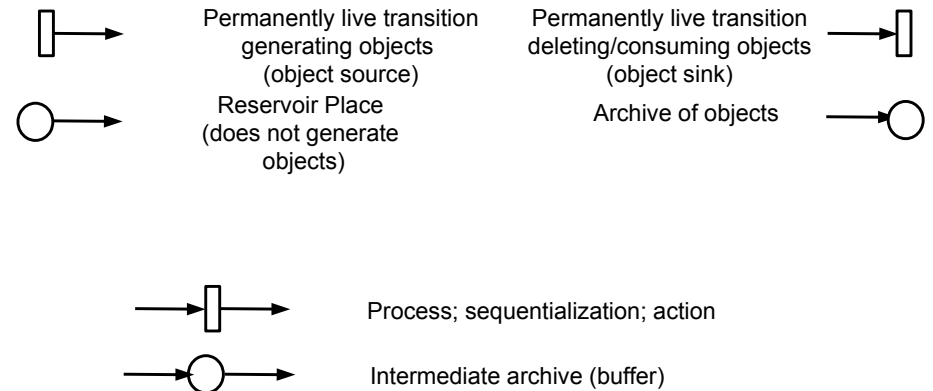


3.2 Patterns in Petri Nets

Analyzability:
 Petri Nets can be analyzed for patterns (by pattern matching)



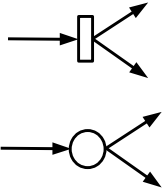
Simple PN Buffering Patterns



Parallelism Patterns

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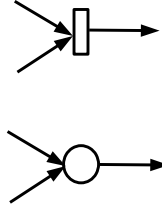


Replication and distribution of objects; forking off parallelism (AND-split)

Forking off parallelism indeterministically (conflict, XOR split)

Joining parallelism synchronization barrier (AND-join)

Collecting objects from parallel processes (OR-join)

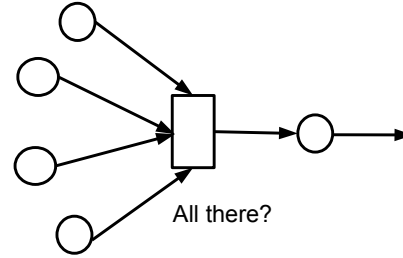


Examples for Building Blocks

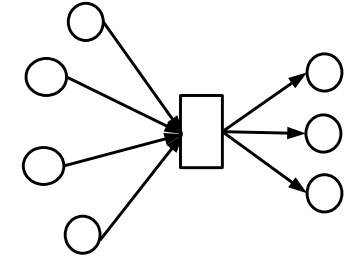
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Synchronization barrier



Bridges: Transitions between phases

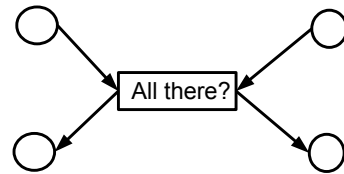


Patterns for Parallelism

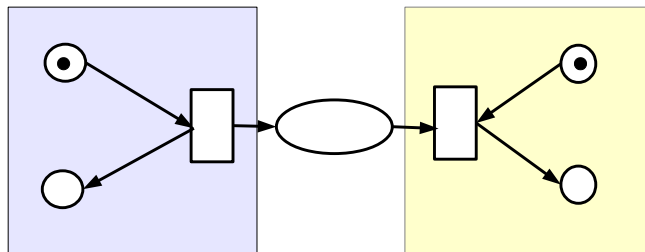
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Coupling processes with parallel continuation



Producer/Consumer with buffer (CSP channel)

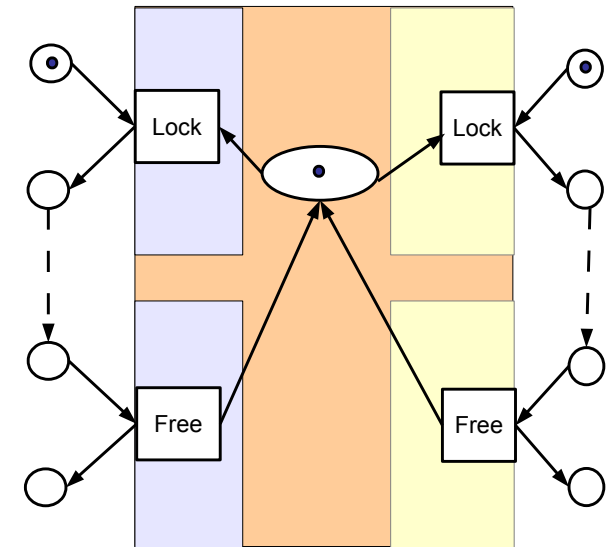


Semaphores For Mutual Exclusion

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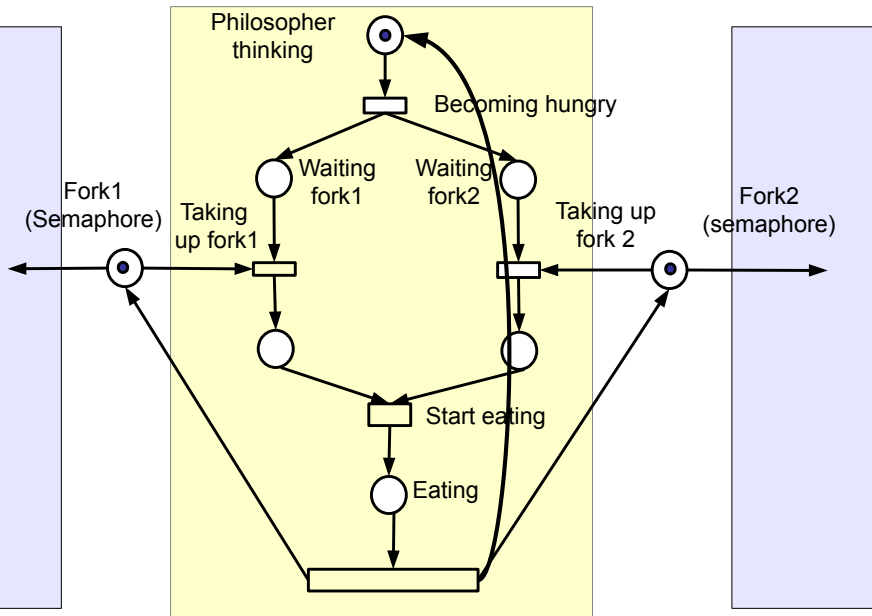
Binary or counting semaphores: depends on the capacity of the semaphore place



Dining Philosophers

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3.3 Refactorings (Reduction Rules) for Petri Nets

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.. in the form of graph rewrite rules



Advantage

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- ▶ Patterns can be used to model specific requirements
- ▶ PN can be checked for patterns by Pattern Matching (Graph Rewriting)
 - Patterns can be restructured (refactorings)
 - Patterns can be composed (composition)
- ▶ Further semantic analysis of PN: Parallel, indeterministic systems can be checked for
 - Absence of deadlocks: will the parallel system run without getting stuck?
 - Liveness: will all parts of the system work forever?
 - Fairness: will all parts of the system be loaded equally?
 - Bounded resources: will the system use limited memory, and how much? (important for embedded systems)
 - Whether predicates hold in certain states (model checking)

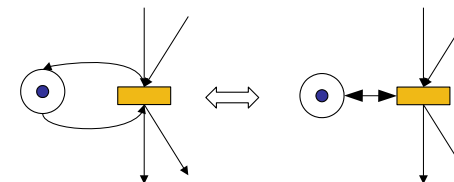


Special Restructuring Patterns (Refactorings)

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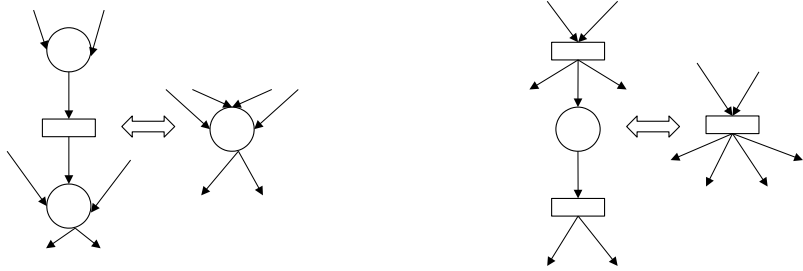
- ▶ *Source transitions* are always enabled, i.e., generate tokens (*token generator*)
- ▶ *Sink transitions* are always enabled and swallow tokens (*token sink*)
- ▶ A *self-loop* is a pair of a place p and a transition t if p is both output and input place of t
 - A PN without any self-loops is *pure*. Its arc relation is irreflexive



Simple Reduction Rules

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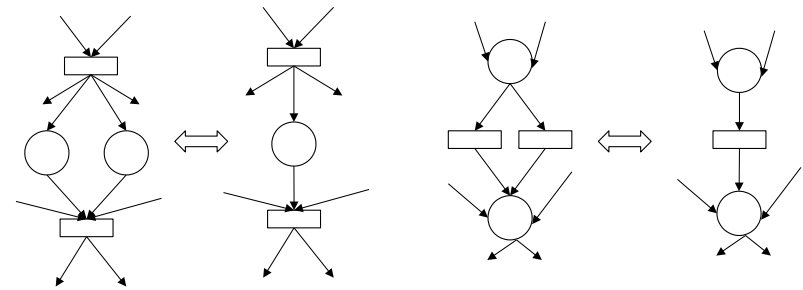


- 1) Fusion of Series Places (FSP) (Bridge elimination)
- 2) Fusion of Series Transitions (FST) (Intermediate buffer elimination)

Simple Reduction Rules

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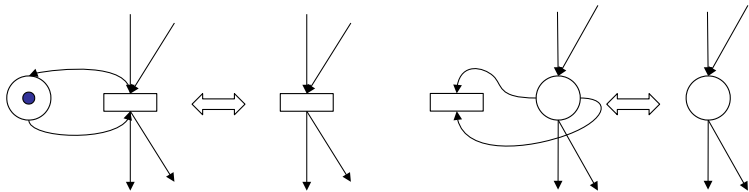
- 3) Fusion of Parallel Places (FPP)
- 4) Fusion of Parallel Transitions (FPT)



Simple Reduction Rules

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- 5) Elimination of Self-loop Places (ESP)
- 6) Elimination of Self-loop Transitions (EST)

All transformations preserve liveness, safeness and boundedness.



3.4 Composability of CPN

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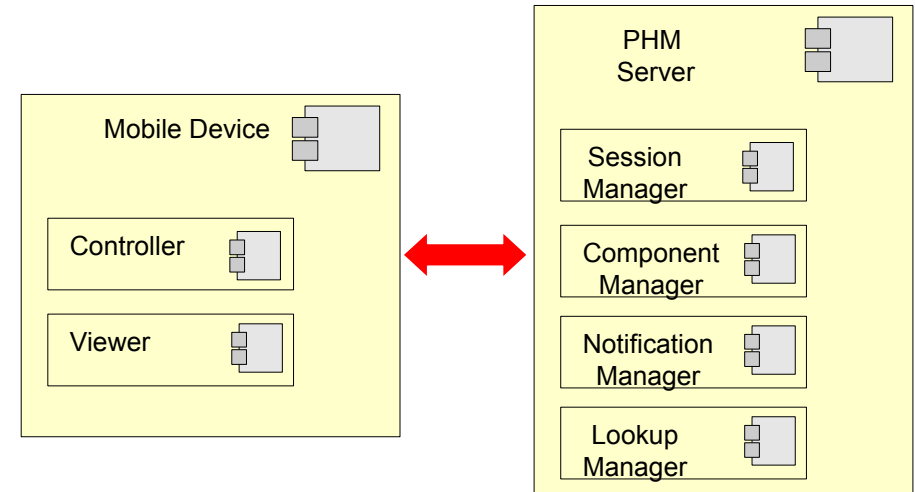


Case Study for Composition: Pervasive Healthcare Middleware (PHM)

- 55
- ▶ in development at the Pervasive Computing Center, University of Aarhus
 - ▶ Basic idea:
 - Specify the structure of an application with UML
 - and the behavior with CPN, describing the behavior of the classes/objects (object lifecycle)
 - Glue behavior together with page glueing mechanism
 - ▶ Electronic patient records (EPR) replace the papers
 - First version in 2004, on stationary PC
 - Next versions for pervasive computing (PDA, wireless):
 - Hospital employees will have access to the patient's data wherever they go, from Xray to station to laboratories
 - For instance, medication plans are available immediately

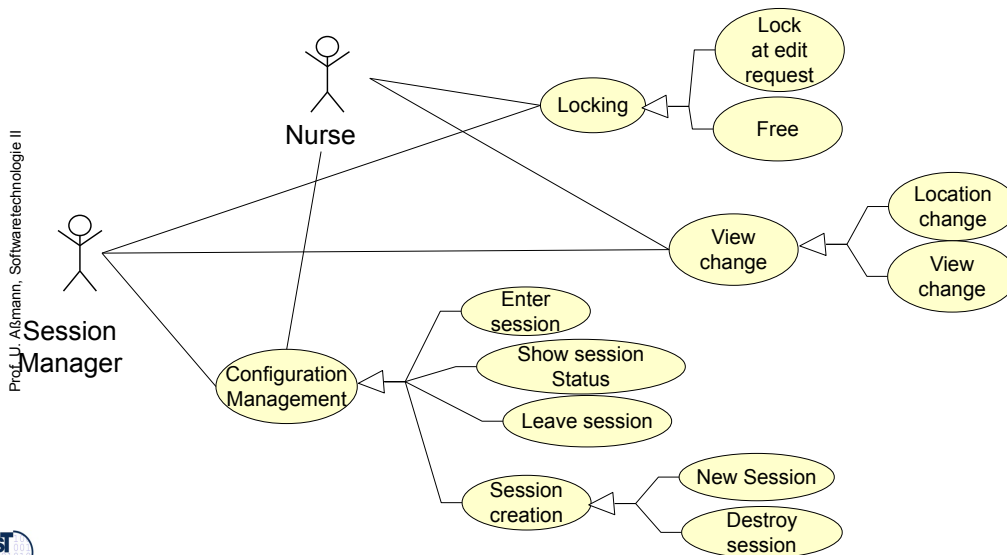
The PHM Architecture

- 56
- ▶ A *session* is entered by several mobile devices that collaborate



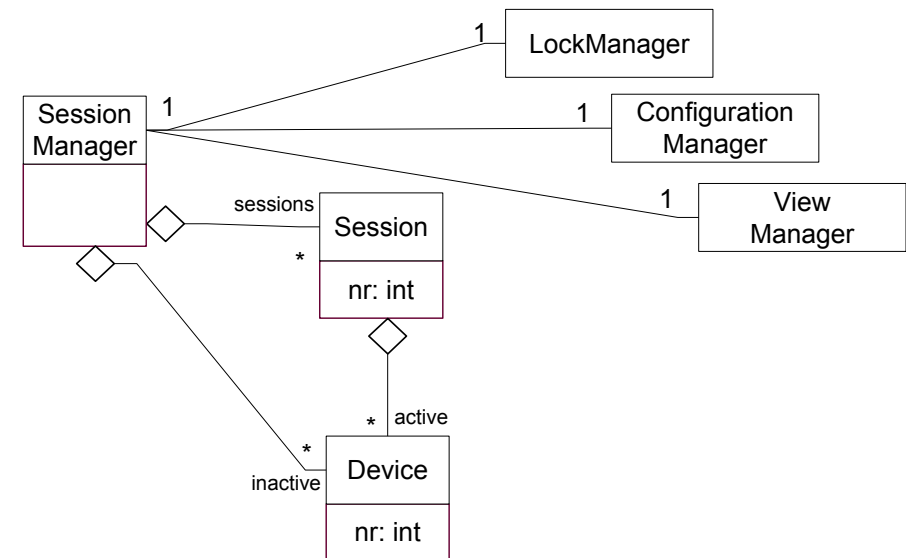
Session Manager Use Cases

- 57
- ▶ The *session manager* manages all mobile devices that collaborate in a certain scenario



Class Diagram Session Manager

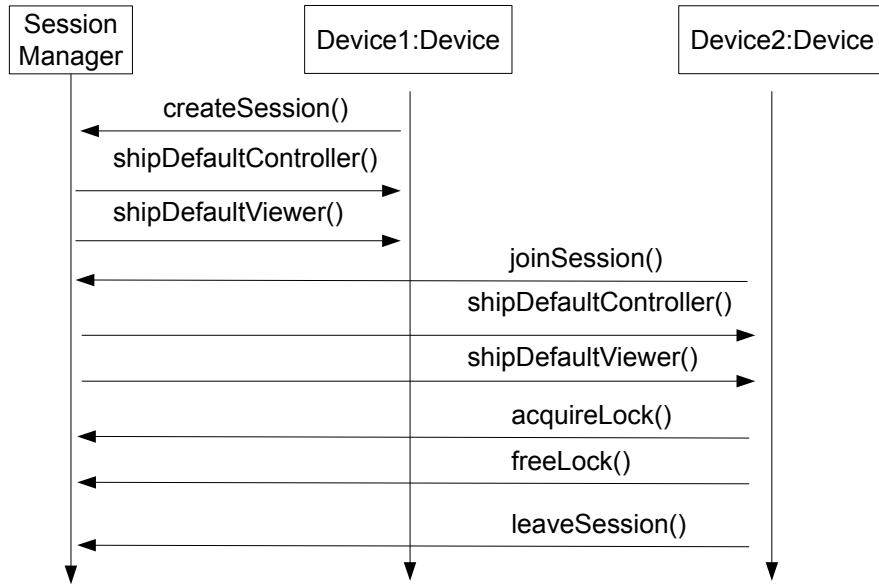
58



Sequence Diagram Session Manager

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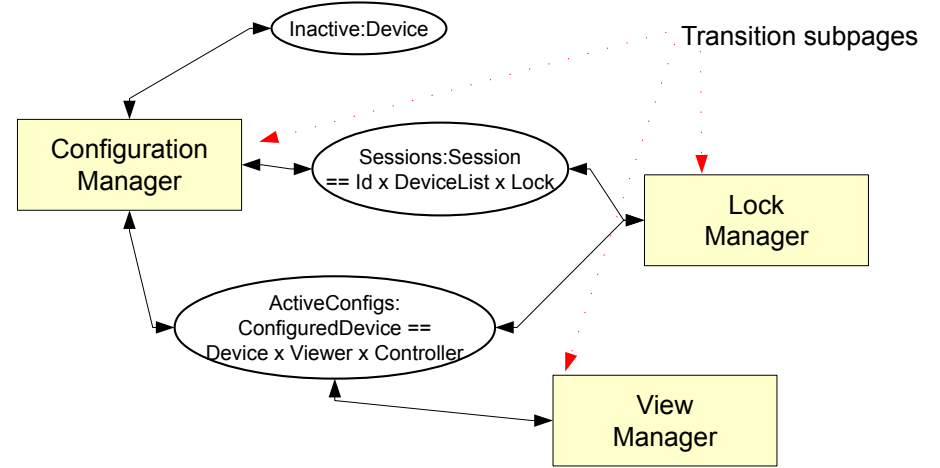


Session Manager Top-Level CPN

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- ▶ Double arrows indicate that arrows run in both directions
- ▶ Basic Types
 - `Session ::= SessionId DeviceList LockType`
 - `ConfiguredDevice ::= Device Viewer Controller`

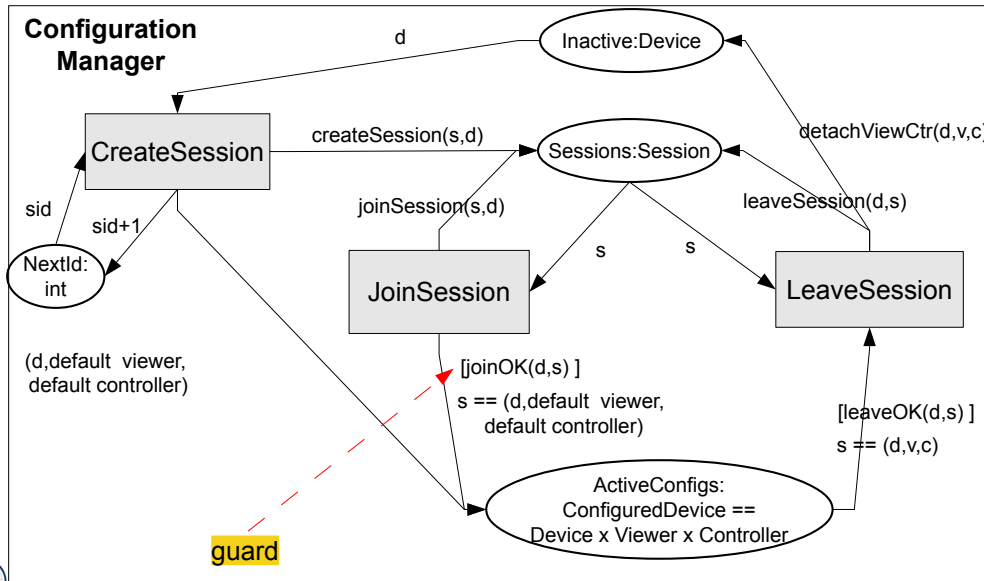


Configuration Manager Page

61

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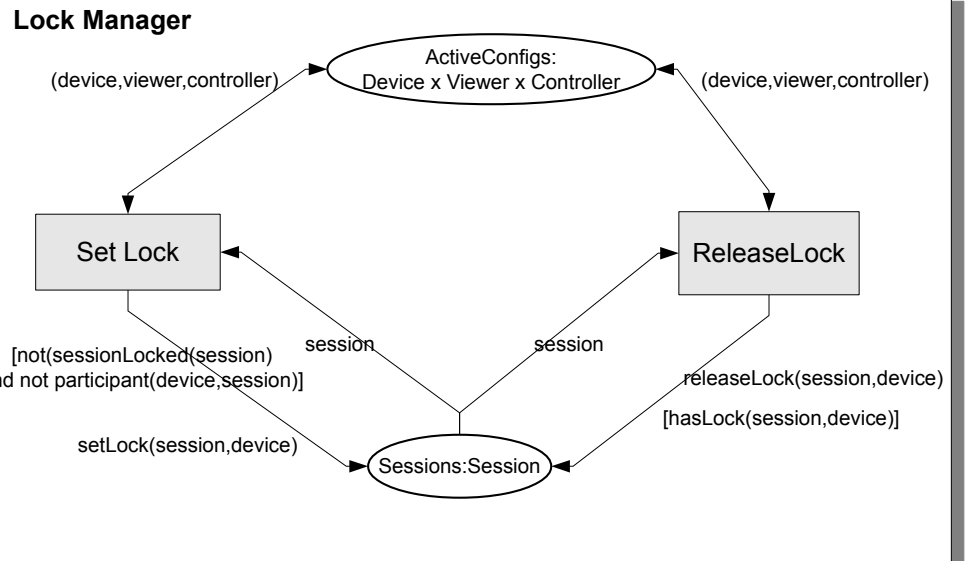
- ▶ Page is fused along common names of nodes

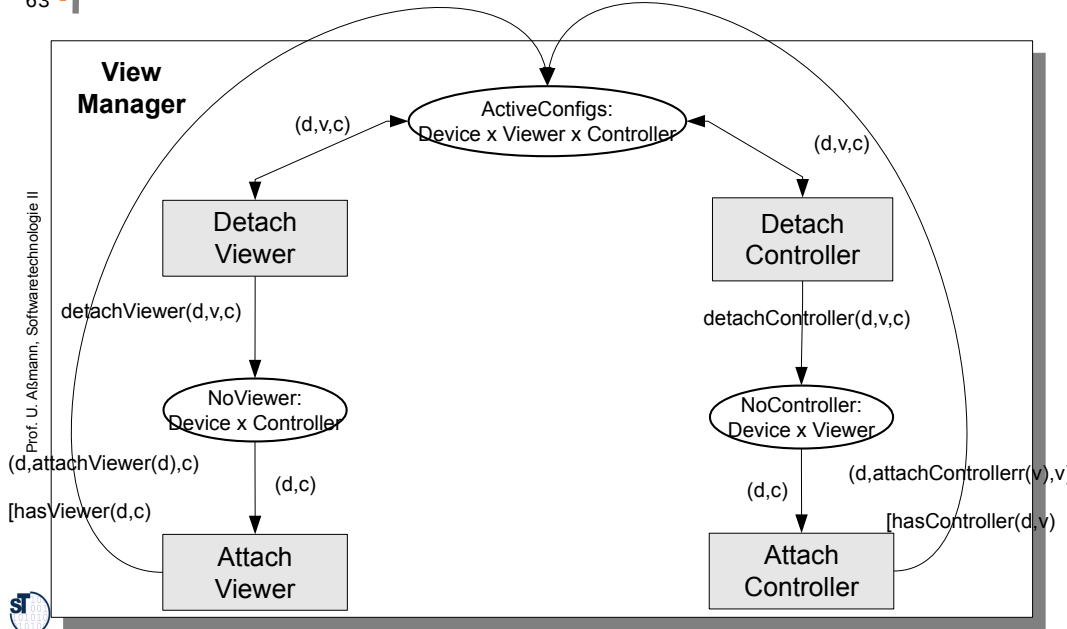


Lock Manager Page

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- ▶ The CPN pages are attached to UML classes, i.e., describe their behavior
 - States and transitions are marked by UML types
- ▶ Every subpage is coupled to others (composed with others)
 - via common states (*fusing/join states*)
 - The union of the pages via join states is steered by OR, i.e., the pages add behavior, but do not destroy behavior of other pages
 - Via common transitions (*fusing/join transitions*)
 - The union of the pages via join transitions is steered by AND, i.e., the pages add behavior and synchronize with transitions of other pages
- ▶ Transitions are interpreted as coarse-grain events
 - On the edges, other functions (actions) are called
 - Hence, CPN are *open*: if something is too complicated to model as a PN, put it into functions

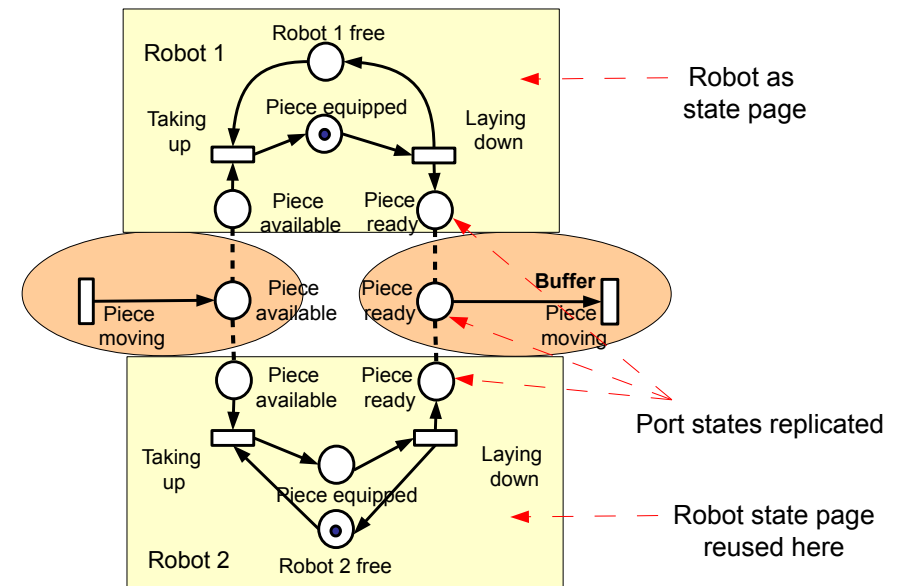


Coupling of Place and Transition Pages

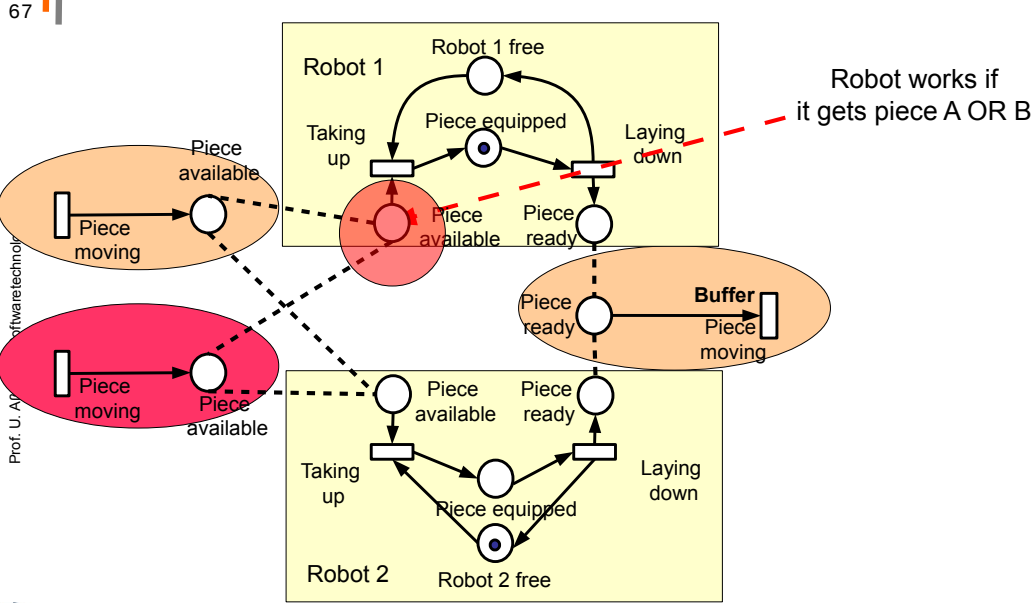
- ▶ **Port state coupling (or fuse, merge, composition):** Place pages are coupled to other place pages via common states (port states)
 - The union of the pages is steered by OR, i.e., the pages add behavior, but do not destroy behavior of other pages
- ▶ **Port transition coupling:** Transition pages are coupled to other transition pages via common transitions (port transitions)
 - The union of the pages is steered by AND, and every page changes the behavior of other page
 - Events must be available on every incoming edge of a transition
 - The transitions of the combined net only fire if the transitions of the page components fire



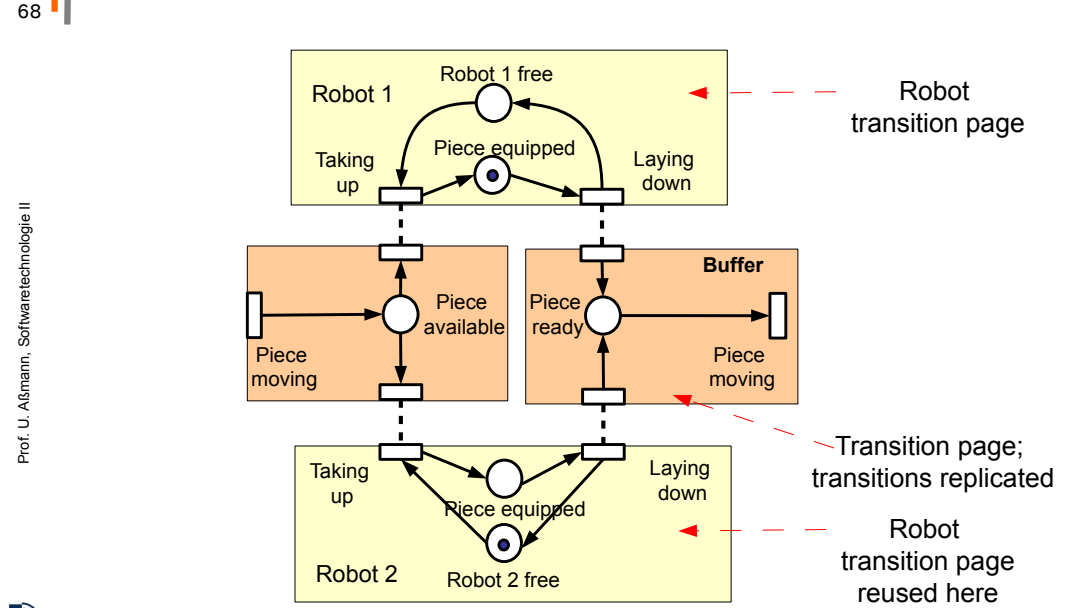
Robots with State Pages, Coupled by Replicated State Ports



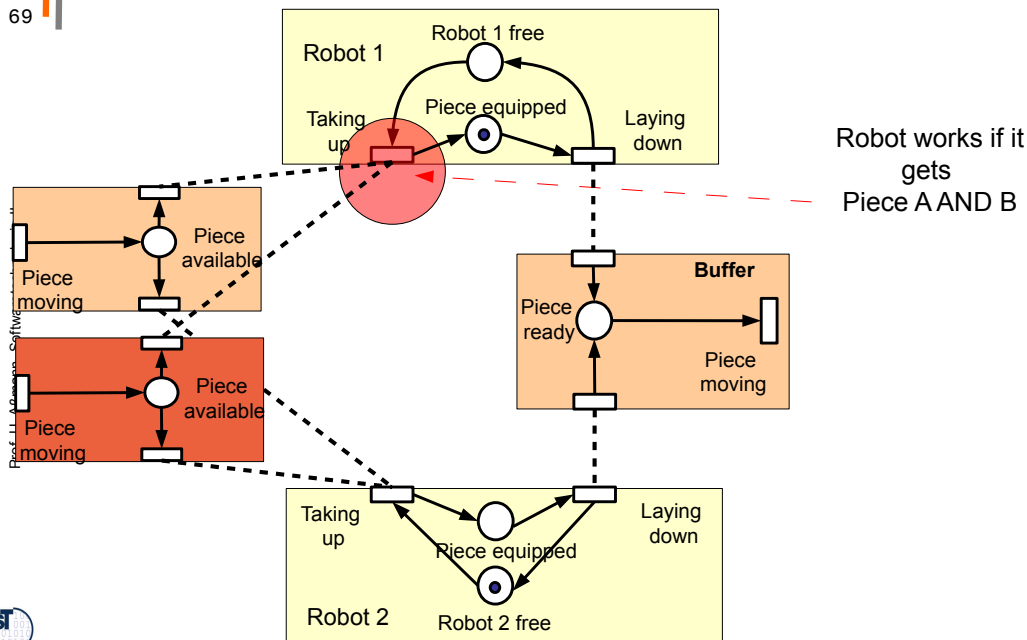
A Robot OR-composed View



Robots with Transition Pages, Coupled by Transition Ports



A Robot AND-composed view



Advantages of CPN for the PHM

- 70
- ▶ The PHM is a distributed and mobile scenario
 - Devices can fail (battery empty, wireless broken, etc)
 - The resulting CPN can be checked on deadlock, i.e., will the PHM session manager get stuck?
 - ▶ Compact specification
 - Usually, CPN are much more compact than statecharts
 - ▶ Variability
 - The pages are modular, i.e., can be exchanged for variants easily (e.g., other locking scheme)
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3.4 Parallel Composition of Colored Petri Nets

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Parallel composition of PN

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- ▶ Complex synchronization protocols can be abstracted to a pattern (als called transition page or a place page)
- ▶ When joining PN with AND (i.e., joining transition pages), synchronization protocols can be overlaid to existing sequential specifications

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Unforeseeable Extensible Workflows

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- ▶ Workflows are described by Colored Petri Nets (CPN) or languages built on top of CPN:
 - YAWL language [van der Aalst]
 - Workflow nets
- ▶ We can use the extension of CPN for workflow composition, enriching a workflow *core* with a workflow *aspect*:
 - **Place extension (State extension):** adding more edges in and out of a place (state):
 - OR-based composition: Core OR view: Core-place is ORed with Aspect-Place
 - **Transition extension (Activity extension):** adding more edges in and out of a transition (activity)
 - AND-based composition: Core-transition is ANDed with Aspect-transition

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Weaving Patterns for Synchronization Protocols with AND Composition

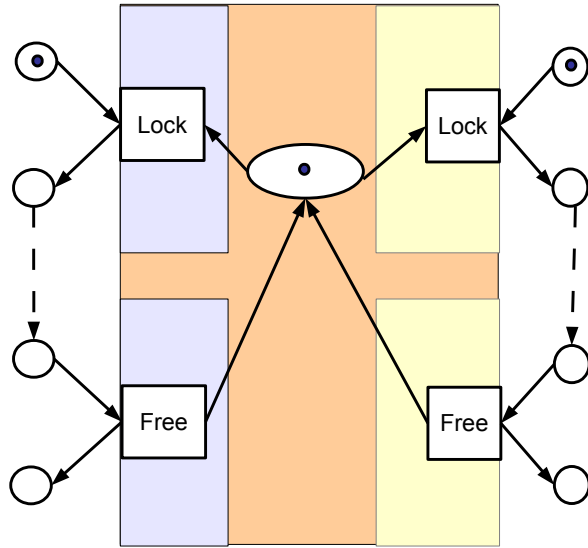
74

- Complex synchronization protocols can be abstracted to a transition page
- Weaving them with AND, they can be overlaid to existing sequential specifications

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Semaphores For Mutual Exclusion Revisited

- 75 ▶ Forms a synchronisation aspect via ANDed Lock transitions



Insight

- 77 ▶ AND-Merge and OR-Merge of CPN are sufficient basic composition operators for building complex aspect weavers for workflow languages built on CPN

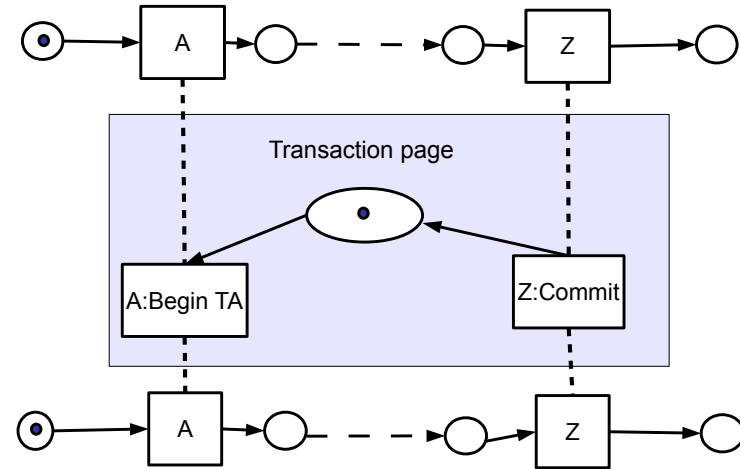
AND-weaving for synchronization

OR-weaving for functional extension



Transaction Protocols as AND-Aspects

- 76 ▶ Crosscut between processes (cores) and transaction protocol (aspect)



3.5 The Application to Modelling

78



Petri Nets Generalize UML Behavioral Diagrams

79

Activity Diagrams

- ▶ Activity Diagrams are similar to PN, but not formally grounded
 - Without markings
 - No liveness analysis
 - No resource consumption analysis with boundness
 - No correspondence to UML statechart, although for PN holds that PN with finite reachability graphs correspond to finite automata
- ▶ I.e., it is difficult to prove something about activity diagrams, and difficult to generate (parallel) code from them.

Data-flow diagrams

- ▶ DFD are special form of activity diagrams, and correspond to Marked Graphs

Statecharts

- ▶ Finite automata are restricted form of Petri nets
- ▶ The hierarchical structuring in Statecharts is available in High-Level Petri Nets (e.g., CPN)

A Simple Modelling Process for Safety-Critical Software with CPN

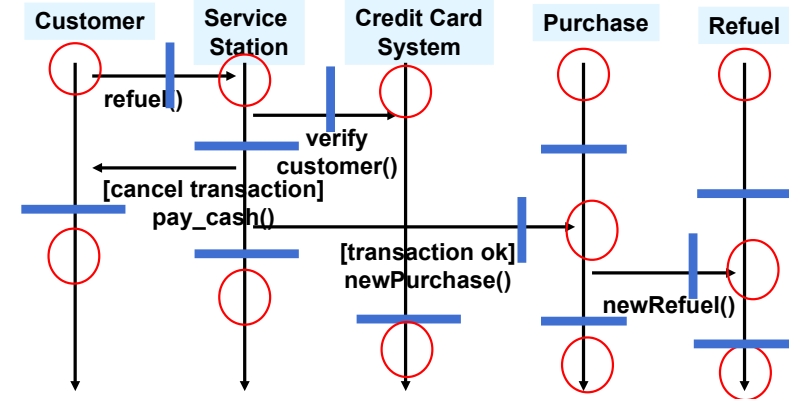
81

- ▶ **Elaboration:** Identify active and passive parts of the system
 - Active become transitions, passive to places
- ▶ **Elaboration:** Find the relations between places and transitions
- ▶ **Elaboration:** How should the tokens look like: boolean? Integers? Structured data?
 - Use UML class diagrams as token type model
- ▶ **Restructure:** Group out subnets to separate "pages"
- ▶ **Refactor:** Simplify by reduction rules
- ▶ **Verify:** Analyse the specification on liveness, boundedness, reachability graphs, fairness. Use a model checker to verify the CPN
- ▶ **TransformRepresentation:** Produce views as statecharts, sequence, collaboration, and activity diagrams..

Petri Nets Generalize UML Sequence Diagrams

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- ▶ The object life lines of a sequence diagram can be grouped into state such that a PN results
- ▶ All of a sudden, liveness conditions can be studied
 - Is there a deadlock in the sequence diagram?
 - Are objects treated fair?



How to Solve the Reactor Software Problem?

82

- ▶ Specify with UML and CPN
 - Verify it with a model checker
 - Let a prototype be generated
 - Test it
 - Freeze the assembler
- ▶ Then, verify the assembler, because you should not trust the CPN tool nor the compiler
 - Any certification agency in the world will require a proof of the assembler!
- ▶ However, this is much simpler than programming reactors by hand...

The Gloomy Future of PN

- 83
- ▶ PN will become the major tool in a future CASE tool or integrated development environment
 - Different views on the PN: state chart view, sequence view, activity view, collaboration view!
 - ▶ Many isolated tools for PN exist, and the world waits for a full integration into UML
 - ▶ CPN will be applied in scenarios where parallelism is required
 - Architectural languages
 - Web service languages (BPEL, BPMN, ...)
 - Workflow languages
 - Coordination languages



The End

- 84
- ▶ Thanks to Björn Svensson for help in making slides, summarizing [Murata]

