

32. GraphWare: Languages for Graph Transformations and Rewriting

Refactoring, Improvement of Large Models

- 1) Graph rewriting
- 2) Complex local graph rewritings
- 3) Context-sensitive graph rewritings
- 4) GrGen
- 5) ATL
- 6) More on the Graph-Logic Isomorphism

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Obligatory Literature

- ▶ Kevin Lano. Catalogue of Model Transformations
 - <http://www.dcs.kcl.ac.uk/staff/kcl/tcat.pdf>
- ▶ Uwe Aßmann. Graph rewrite systems for program optimization. ACM Transactions on Programming Languages and Systems (TOPLAS), 22(4):583-637, June 2000.
 - <http://portal.acm.org/citation.cfm?id=363914>
- ▶ Tom Mens. On the Use of Graph Transformations for Model Refactorings. GTTSE 2005, Springer, LNCS 4143
 - <http://www.springerlink.com/content/5742246115107431/>

Other References

- ▶ Uwe Aßmann. OPTIMIX, A Tool for Rewriting and Optimizing Programs. In Graph Grammar Handbook, Vol. II. Chapman-Hall, 1999.
- ▶ K. Lano. Catalogue of Model Transformations
 - <http://www.dcs.kcl.ac.uk/staff/kcl/tcat.pdf>

Other Literature

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Model-Driven Software Development in Technical Spaces (MOST)

- ▶ Frédéric Jouault and Ivan Kurtev. On the Architectural Alignment of ATL and QVT. In: Proceedings of the 2006 ACM Symposium on Applied Computing (SAC 06). ACM Press, Dijon, France, chapter Model transformation (MT 2006), pages 1188–1195.

- <http://atlanmod.emn.fr/bibliography/SAC06a>

- ▶ Tutorial über ATL “Families2Persones”

- http://www.eclipse.org/m2m/atl/doc/ATLUseCase_Families2Persons.ppt

- ▶ ATL Zoo von Beispielen

- <http://www.eclipse.org/m2m/atl/atlTransformations>

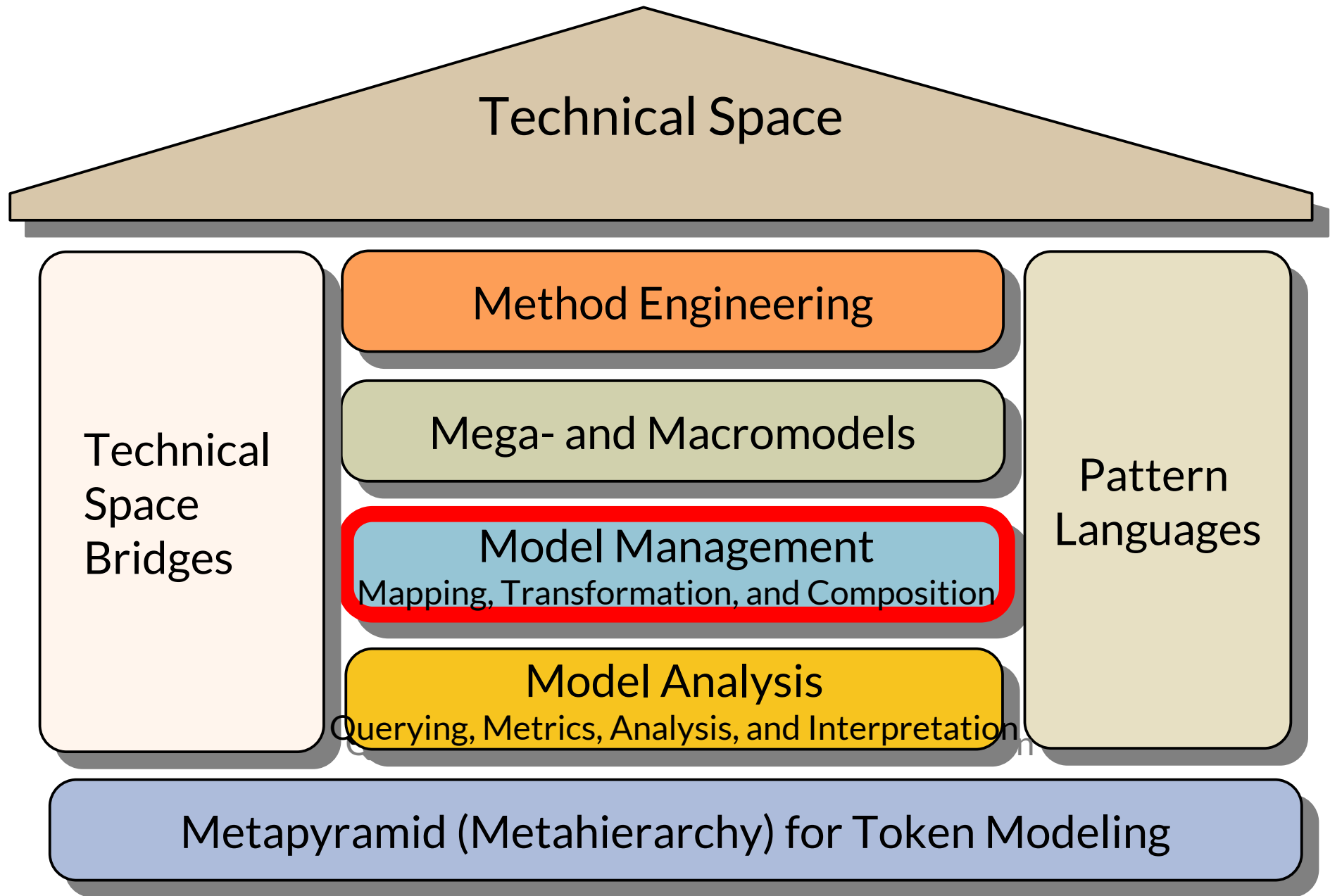
- ▶ A Comparison of ATL and Story-Driven Modeling (Fujaba-style GRS)

http://www.es.tu-darmstadt.de/fileadmin/download/publications/spatzina/PP_AGTIVE_2011.pdf

- ▶ Implementation in ATL

- <http://www.eclipse.org/m2m/atl/atlTransformations/EquivalenceAttributesAssociations/EquivalenceAttributesAssociations.pdf>

Q10: The House of a Technical Space





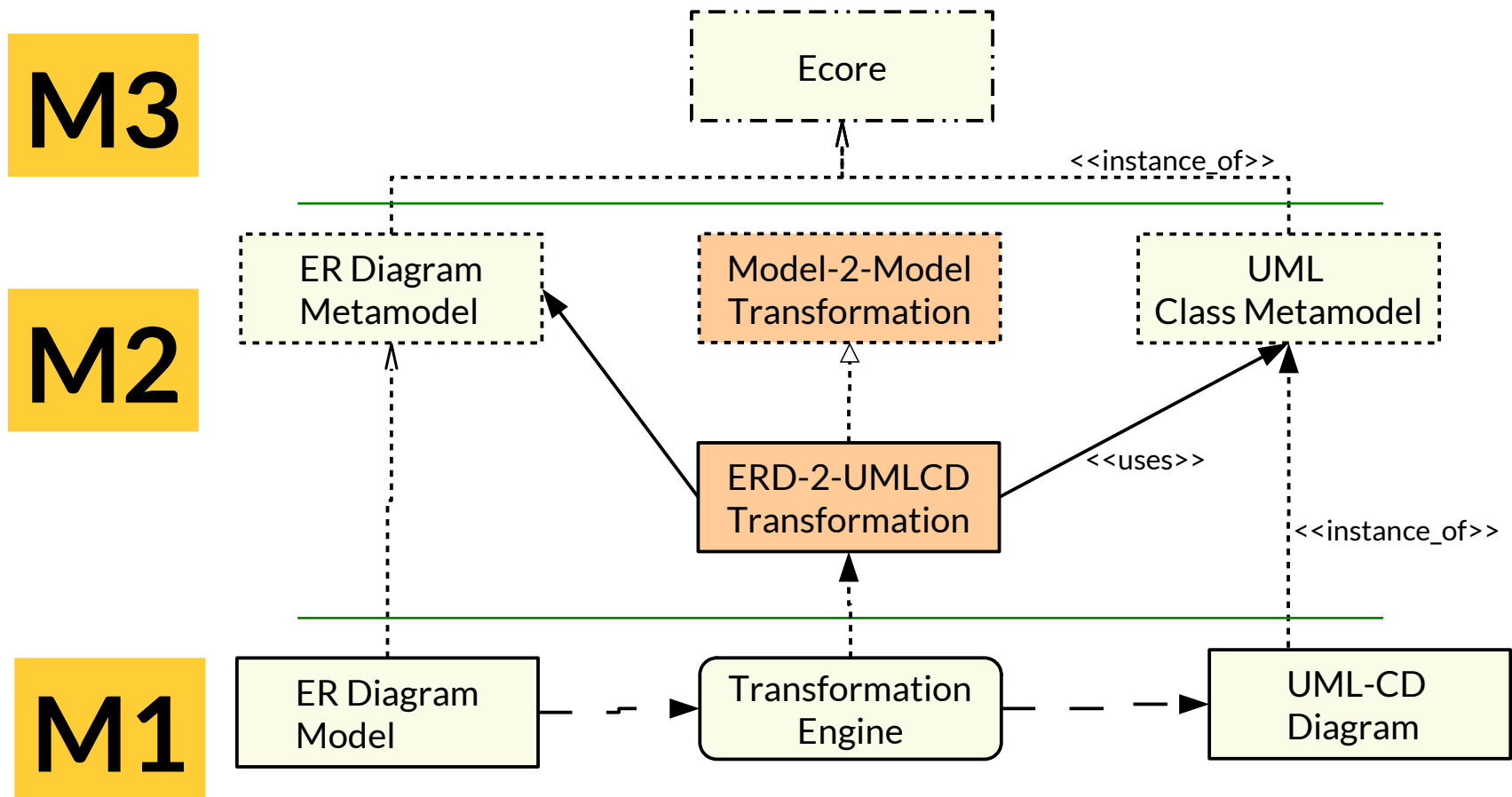
32.1. Graph Rewriting for Code and Model Creation, Transformations, Translation

Model Transformations and Their Metamodels

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Model-Driven Software Development in Technical Spaces (MOST)

- ▶ Model transformations defined in Layer M_{i+1} specify how to transform models on M_i
 - Source and target metamodel are connected by a metamodel of a rule-based transformation language
- ▶ **Benefit:** Transformation can be reused for all models, which are instances of the source meta-model



Needs of Graph Rewriting

- ▶ M3: Graph-enabling Metalanguage (Ecore, MOF, ERD, RDFS, OWL)
- ▶ M2: Metamodel for Nodes and Edges (DDL)
 - MOF, EMOF, tool-specific, etc.
- ▶ M2: Metamodel for Rule Language
 - LR Form (left to right rule)
 - Fujaba Storyboard Notation
 - GrGen metamodel
- ▶ M1: Node and edge allocators (factories)
 - Graph libraries such as Jgrapht.org
- ▶ M0: graph pools with nodes and edges
 - To limit rewriting

Applications of Graph Rewrite Systems for *Transformations* (Graphersetzungssysteme)

- ▶ Interpretation of code and models [Rensink]
- ▶ MDSD tools need model transformations
 - Model transformations (Alexander Christoph)
 - Model aspect weaving (Aßmann, Heidenreich, many others)
 - Creation of more specific models in MDA, including the computation of trace create links [Taentzer]
 - Refinement in design [Lano, Schürr, Lewerentz]
 - Refactoring [Mens]
- ▶ Compilation and Translation of code and models [Nagl, Aßmann]
- ▶ Analysis [Reps]
 - Interprocedural analysis with graph reachability
- ▶ Optimization [Aßmann]
 - Global code transformations, such as lazy and busy code motion (loop invariant code motion)
 - message optimization
- ▶ Configuration management [Westfechtel]

Model Transformation and Optimization with Graph Rewriting

- ▶ Use the **graph-logic-isomorphism** [Courcelle]: Represent everything in a program or a model as directed graphs
 - Program code (control flow, statements, procedures, classes)
 - Model elements (states, transitions, ...)
 - Analysis information (abstract domains, flow info ...)
- ▶ Directed graphs with node and edge types, node attributes
 - one-edge condition (no multi-graphs)
- ▶ Use edge addition rewrite systems (EARS) to query, analyze, map the graphs to each other
- ▶ Use graph rewrite systems (GRS) to create, construct, and augment the graphs
 - Transform the graphs
 - Generate code
- ▶ Preferably, the GRS should terminate (XGRS, exhaustive GRS)

Specification Process For Transformation with Deep Analysis

1) Specification of the data model (graph schema)

- Specification of the graph schema with a graph-like DDL (ERD, MOF, GXL, UML or similar):
 - **Schema of the program representation:** program code as objects and basic relationships. This data, i.e., the start graph, is provided as result of the parser
 - **Schema of analysis information** (the inferred predicates over the program objects) as objects or relationships

2) „Flat“ program analysis (preparing the abstract interpretation)

- Querying graphs, enlarging graphs
- Materializing implicit knowledge to explicit knowledge

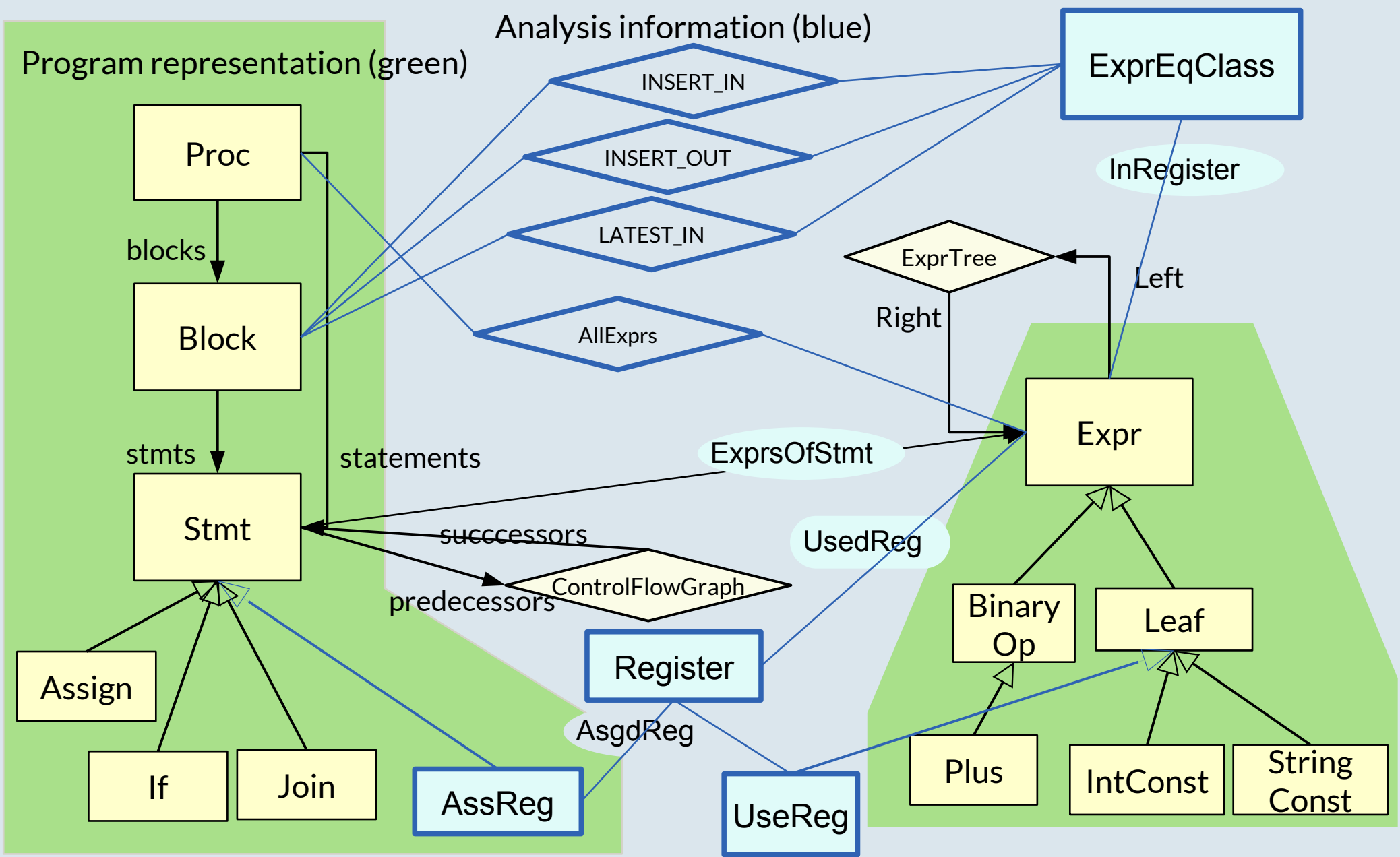
3) „Deep Analysis“: Abstract Interpretation (program analysis as interpretation)

- Specifying the transfer functions of an abstract interpretation of the program with graph rewrite rules on the analysis information

4) Program transformation (optimization)

- Transforming the program representation

Q14: A Simple Program (Code) Model (Schema) in MOF



GrGen Metalanguage

- ▶ GrGen has a metalanguage / DDL similar to MOF, with
 - node, edge, and graph types with inheritance
 - named rules with many flavours, can be called like procedures
 - negative application conditions
 - alternatives
 - iterations
- ▶ Try to specify the MOF metamodel of the last slide in GrGen DDL

32.1.1 Introduction to Storyboard Rule Notation

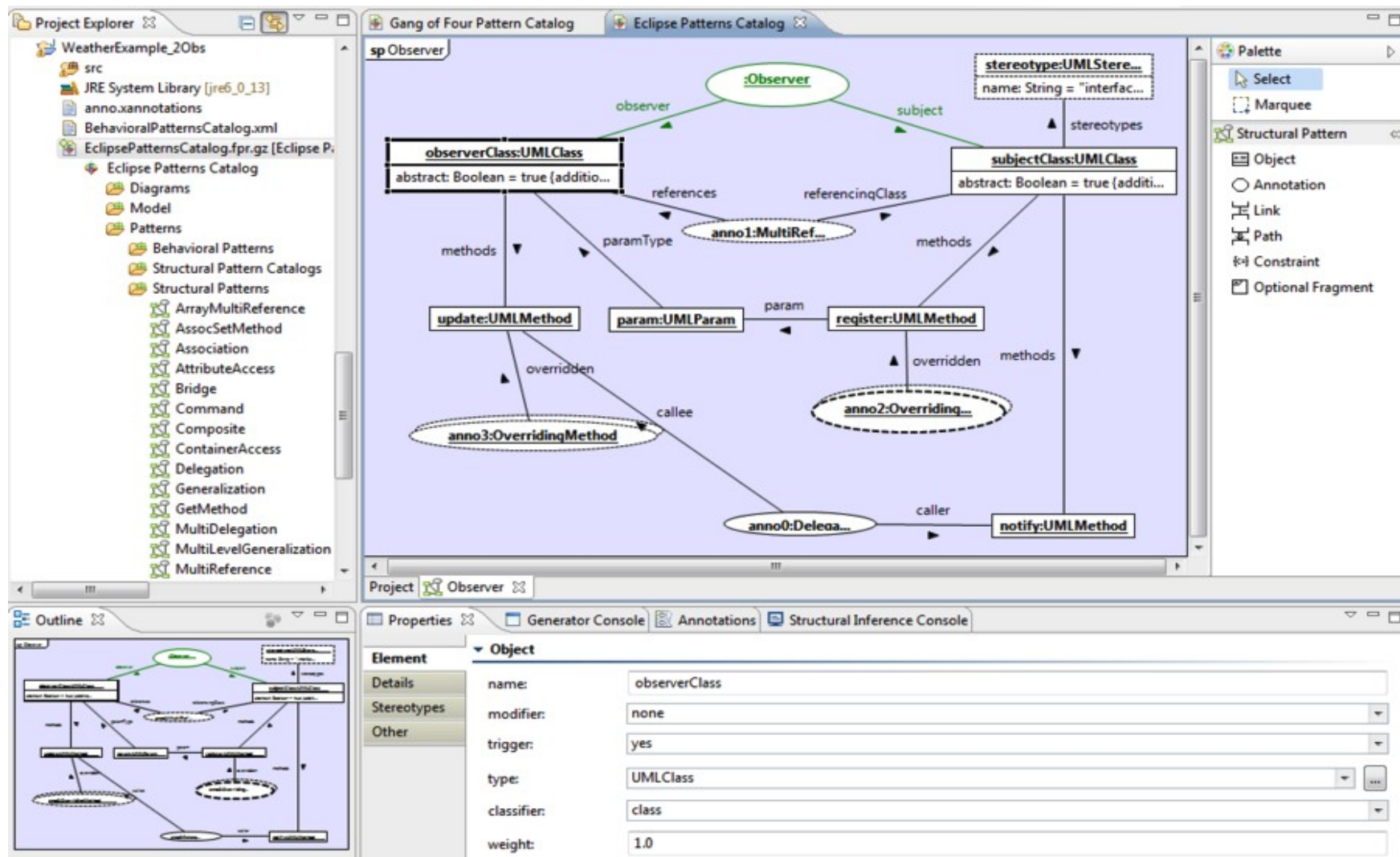
Originally introduced by Fujaba www.fujaba.de (tool now unsupported)



DRESDEN
concept
Exzellenz aus
Wissenschaft
und Kultur

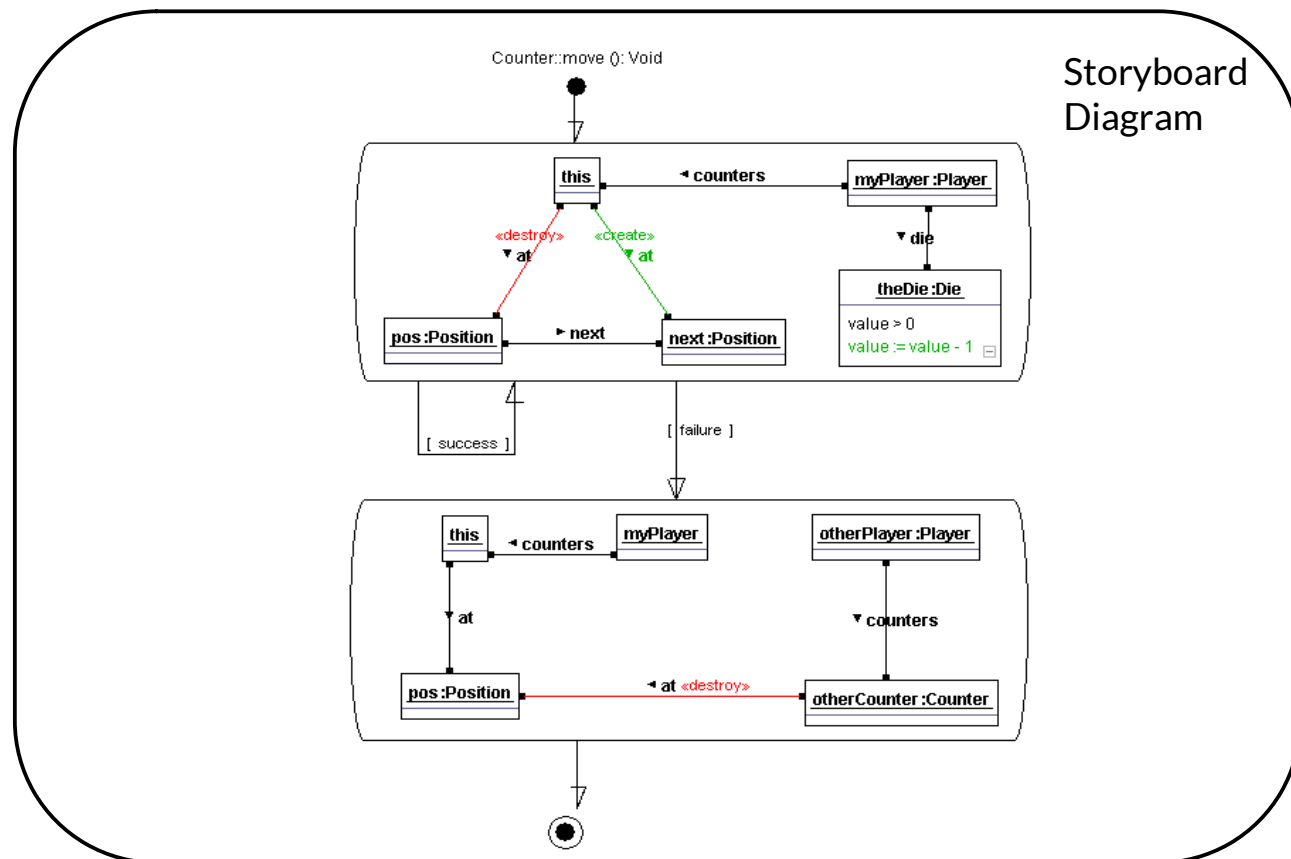
Fujaba

- ▶ Fujaba is a MetaCASE-tool based on GRS with home-grown metalanguage and metamodel
- ▶ Basic technology: graph pattern matching and rewriting



Fujaba Storyboard Diagrams for Adding and Removing Graph Fragments

- ▶ Storyboards are activity diagrams in which activities are GRS
- ▶ **Green** color: adding model fragments; **Red** color: deleting them
- ▶ Pool starts at node this and reaches into the object net
- ▶ GRS can be embedded into Petri Nets, DFG and other BSL



32.2. Complex Local Graph Rewritings

- On Dags (with joins) and Graphs (with cycles)

Code Optimizations Expressible by Local Graph Rewritings

- ▶ Local transformations of the program representation
 - copy propagation, constant propagation
 - loop optimizations (unrolling etc.)
 - branch optimization
 - strength reduction
 - idiom recognition (pattern matching of complex patterns)
 - dead code elimination

- ▶ Transformations of the inheritance hierarchy
 - Flattening (Reachability)
 - Removal of redundant inheritances
 - Refactorings
 - Split classes
 - Merge classes
 - Move class
- ▶ Support during refinement
 - Flattening aggregation, composition, multiple inheritance
- ▶ Optimizations:
 - Peephole optimizations (local transformations)
- ▶ Generation of dependent models

Example: Peephole Transformation “Local Sharing of Equivalent Subexpressions”

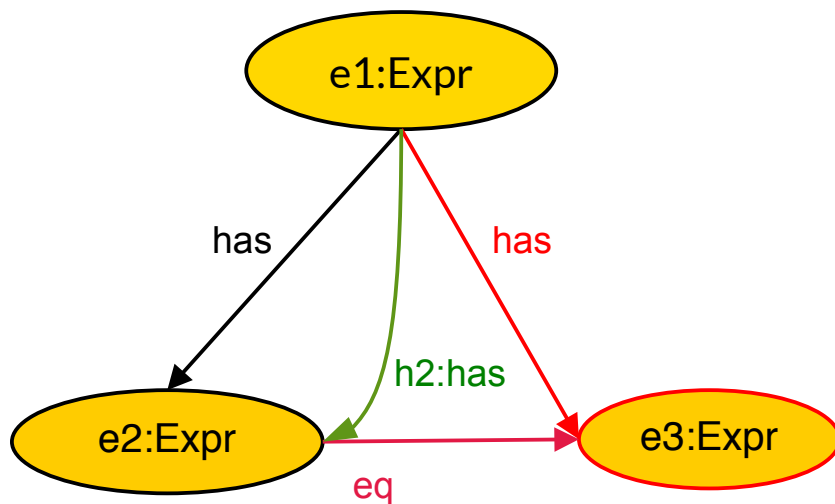
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Model-Driven Software Development in Technical Spaces (MOST)

```
if has(Expr1, Expr2),  
  has(Expr1, Expr3),  
  eq(Expr2,Expr3)  
then  
  delete Expr3;  
  h2:has(Expr1,Expr3)  
;
```

- ▶ Share common subexpressions

```
// GrGen  
rule foldCommonSubexpression(e1:Expr) {  
  e1 -:has-> e2:Expr;  
  e1 -:has-> e3:Expr;  
  e2 -:eq->e3;  
  modify { e1:-h2:has-> e2 }  
}
```

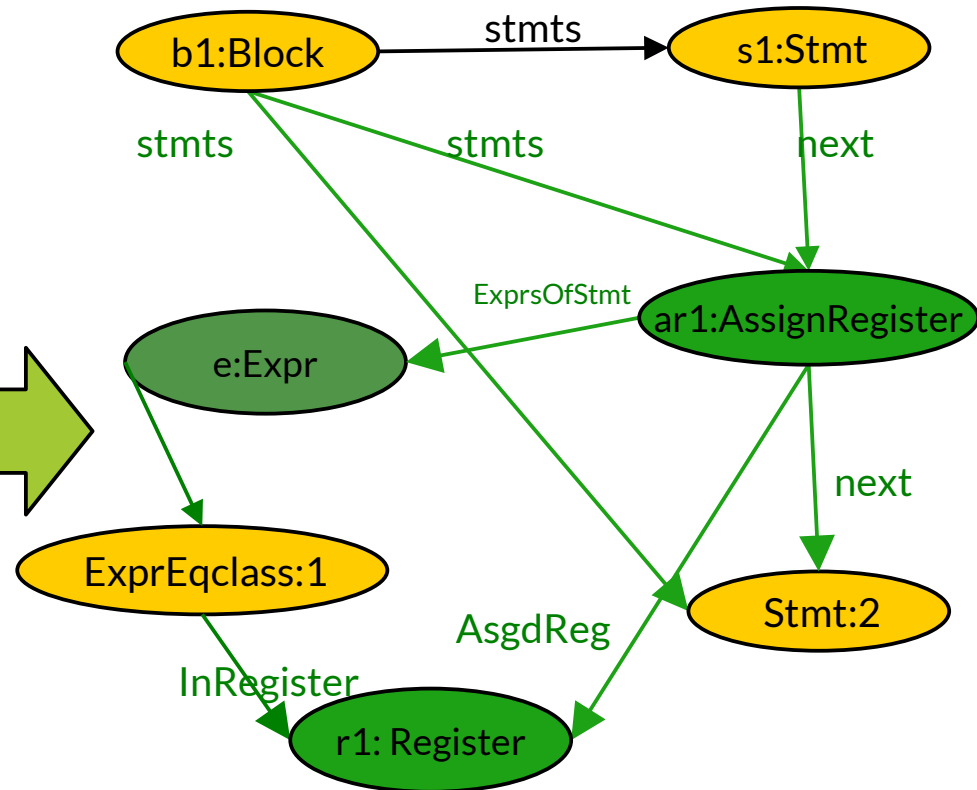
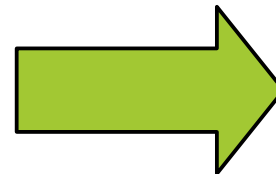
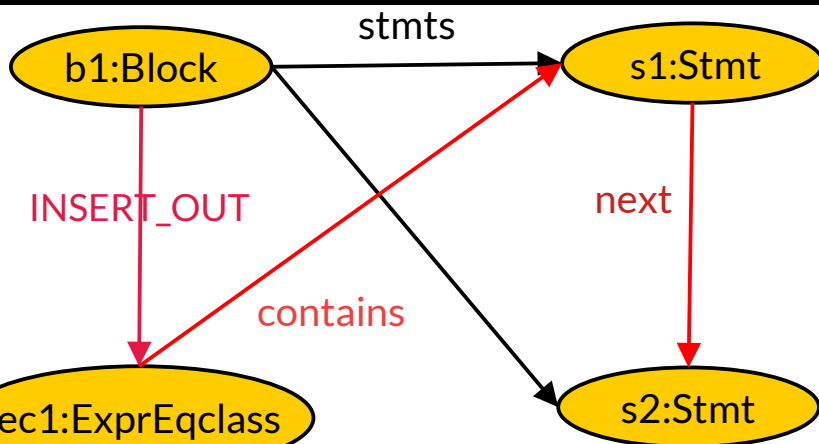


Example: Lazy Code Motion Transformation (in LR Form)

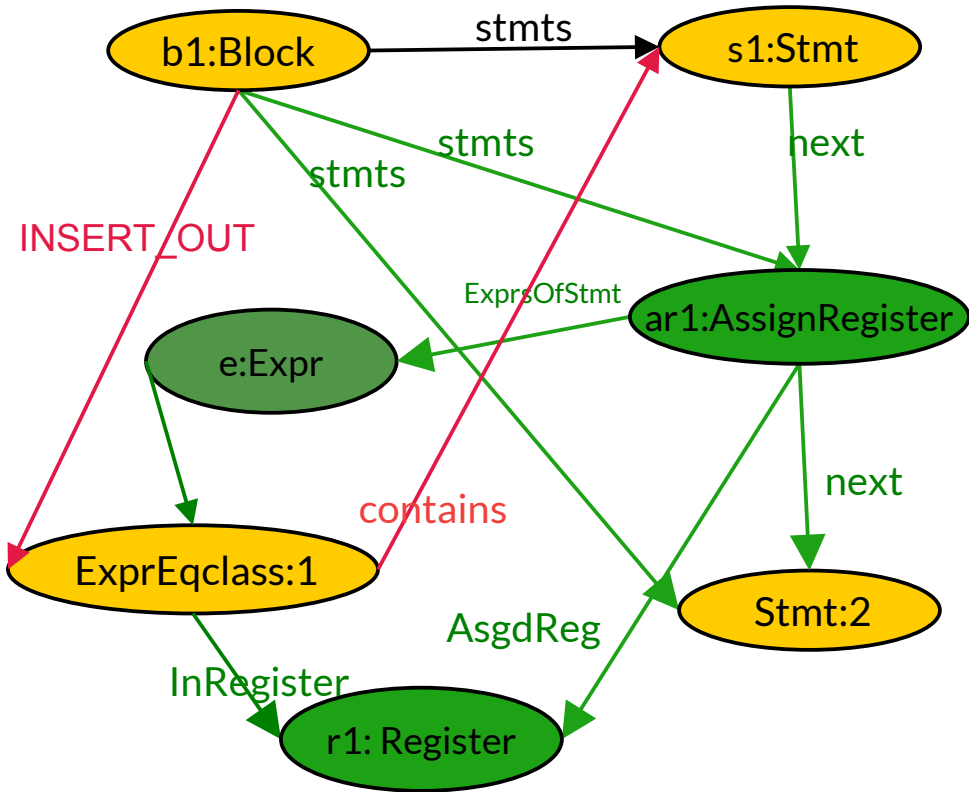
```
// GrGen
rule insertAssignRegisterAtBlockOUT (b1:Block) {
  b1 -:stmts-> s1:Stmt; s1 -:next-> s2:Stmt;
  b1 -:INSERT_OUT-> ec1:ExprEqclass;
  ec1 -:contains-> s1
  modify {
    new r1:Register; new e:Expr;
    new ar:AssignRegister;
    b1 -:Stmts-> ar;
    s1 -:next-> ar; ar -:next->s2
    ec1 -:InRegister-> r1:Register;
    ar -:AsgdReg->r1, ar -:ExprsOfStmt->s2;
    ar -:ExprsOfStmt->e;
  }
}
```

[Aßmann00]

- ▶ Insert expressions at an optimally early place and insert register assignments (ar.AssignRegister) into statement list
- ▶ INSERT_OUT indicates, at which block-exit an expression should be made available

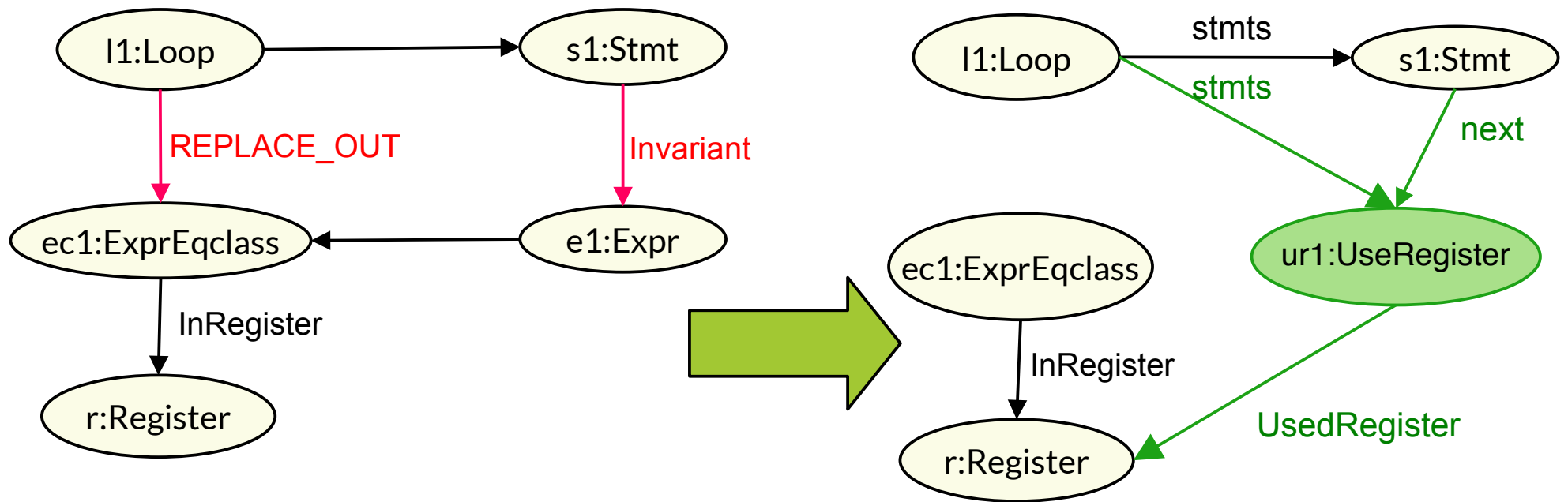


Example: Lazy Code Motion Transformation in Storyboard Notation



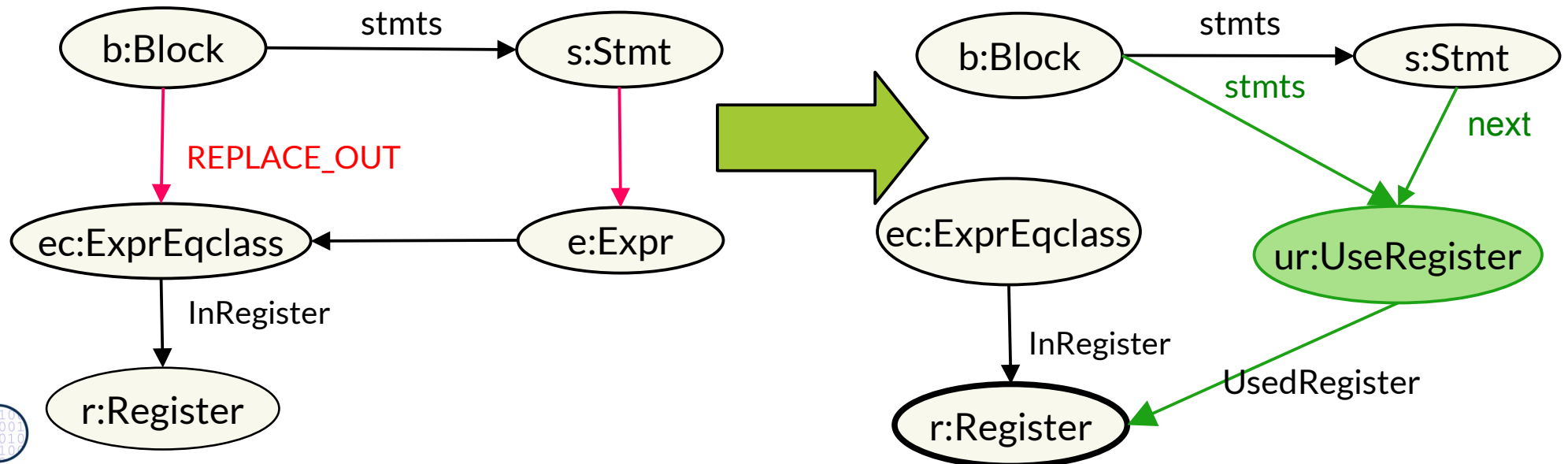
Loop Invariant Code Motion

- ▶ Loop-invariant code motion moves code before loops which is over and over computed again in the loop (loop-invariant)
- ▶ Inserts UseRegister instructions which reuse expression results previously stored in registers



Lazy Code Motion Transformation

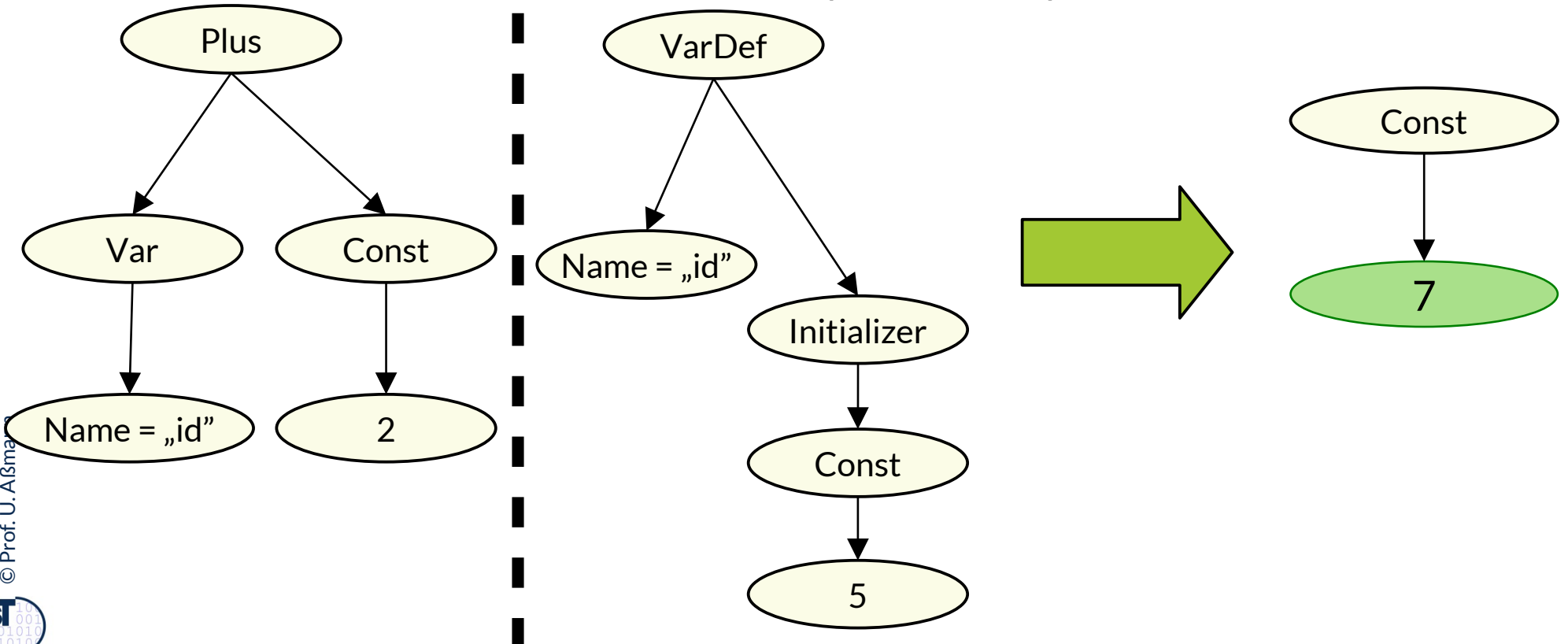
- ▶ REPLACE_OUT indicates at which block-exist an expression should no longer be computed, but its result should be re-used from a register



32.3. Context-Sensitive Rewritings

Extended Constant Folding as Subtractive GRS

- ▶ A term rewrite system usually works context-free, i.e., matches and rewrites only one term.
- ▶ [Lano] mostly has local rewrite rules, but context-sensitive matching is possible
- ▶ A **context-sensitive rewriting** matches a non-connected left-hand side graph with a redex.
 - Matching of one redex can be done in quadratic time, because non-connected nodes have to be pairwise compared



32.4. Model Transformations with GrGen (Karlsruhe)

[GrGenManual] Edgar Jakubeit, Jakob Blomer, Rubino Geiß, The GrGen.NET User Manual Refers to GrGen.NET Release 4.4.2

- www.grgen.net
- <http://www.info.uni-karlsruhe.de/software/grgen/>

- ▶ GrGen is one of the fastest graph transformation tools around
 - Proprietary DDL `grgen.gm` similar to MOF (multiple inheritance, uni-, bidirectional)
 - Textual syntax
 - Interpreter (shell)
 - Visualizer
- ▶ Powerful language
 - Nesting of rules
 - Alternative subrules
 - Negated rules
- ▶ The following examples stem from [GrGenManual]

GrGen Shell Language

- ▶ GrGen has an interactive shell in which graphs can be
 - allocated
 - layouted for print (show graph)
 - rewritten by graph rewriting procedures

```
// creating a state machine in GrGenShell
new graph removeEpsilons "StateMachineGraph"
new :StartState($=S, id=0)
new :FinalState($=F, id=3)
new :State($="1", id=1)
new :State($="2", id=2)
new @(S)-:Transition(Trigger="a")-> @("1") new @("1")-:Transition(Trigger="b")->
@("2") new @("2")-:Transition(Trigger="c")-> @(F) new @(S)-:EpsilonTransition-> @("2")
new @("1")-:EpsilonTransition-> @(F) new @(S)-:EpsilonTransition-> @(F)
show graph ycomp
```

Definition of Context-oriented Petri Nets in GrGen Shell Graph Definition Language (DDL)

```
// Context-oriented Petri Nets

node class ContextNet extends NIdent {

}

edge class contexts

    connect ContextNet[+] --> Context[1];

node class Context extends NIdent {

    active: int = 0;

    bound: int = 1;

}

// weak inclusion relation of contexts: on activation/deactivation trigger this with target

// act(source) -> act(target); deact(source) -> deact(target)

// act(target) ->; deact(target) ->

directed edge class weak_inclusion    connect Context[*] --> Context[*];

// exclusion: both contexts cannot be active at same time

// act(source) -> deact(target)

// act(target) -> deact(source)

undirected edge class exclusion      connect Context[*] -- Context[*];

directed edge class composition      connect Context[*] --> Context[*];
```

Definition of Context-oriented Petri Nets in GrGen Shell Graph Definition Language (DDL) (ctd)

```
// strong inclusion : when target gets deactivated, the source also
// empty triangle
// act(source) -> act(target)
// deact(source) -> deact(target)
// act(target) ->
// deact(target) -> deact(source) -> deact(target)
directed edge class strong_inclusion // full triangle
    connect Context[*] --> Context[*];

// requirement: context can only be activated when target is already
// empty triangle
// act(source) -> only if already: act(target)
// deact(source) ->
// act(target) ->
// deact(target) -> deact(source)
directed edge class requirement // inverse full triangle
    connect Context[*] --> Context[*];
```

GrGen Shell Language for Allocating Graphs

```
new cign:Context(id="Ignore")
new clow:Context(id="LowBattery")
new chig:Context(id="HighBattery")
new cvid:Context(id="VideoCall")
new cdon:Context(id="DoNotDisturb")
new cred:Context(id="Redirect")
new cemu:Context(id="Emergency+Unavailable")
new cfro:Context(id="FrontCamera")
new cuna:Context(id="Unavailable")

# edges

new cign-:exclusion-cuna
new cign-:exclusion-cred
new cuna-:exclusion-cred
new clow-:exclusion-chig

new clow-:weak_inclusion->cign
new cred-:weak_inclusion->cdon
new cvid-:strong_inclusion->cfrz
```


Test Rules Check Conditions in the Graph

```
#using „stateMachine.gm“  
  
test checkStartState { x:StartState;  
    negative { x;  
        y:StartState; }  
}  
  
test checkDoublettes { negative {  
    x:State -e:Transition-> y:State;  
    hom(x,y);  
    x -doublette:Transition-> y;  
    if {typeof(doublette) == typeof(e);}  
    if { ((typeof(e) == EpsilonTransition)  
        || (e.Trigger == doublette.Trigger)); }  
}  
}
```

Normal Rules with Nested Alternatives

```
rule foldCond {  
    cond:Cond -df0:Dataflow-> c0:Const;  
    falseBlock:Block -falseEdge:False-> cond;  
    trueBlock:Block -trueEdge:True-> cond;  
  
    alternative {  
        TrueCond {  
            if { c0.value == 1; } modify {  
                delete(falseEdge);  
                -jmpEdge:Controlflow<trueEdge>->; }  
        }  
        FalseCond {  
            if { c0.value == 0; } modify {  
                delete(trueEdge);  
                -jmpEdge:Controlflow<falseEdge>->; }  
        }  
    }  
  
    modify { delete(df0); jmp:Jump<cond>; }  
}
```

32.4. Model Transformations with ATL

ATLAS Transformation Language (ATL)
<http://www.eclipse.org/atl/>

Tools for Model-Driven Software Development

- ▶ In MDSD and MDA, horizontal and vertical model transformations should be specified with graph rewrite systems
- ▶ Example tools:
 - JastAdd RAGs (Java)
 - GrGen (C#)
 - **ATL** in Eclipse EMOF

ATL Integrates OCL as Query Language

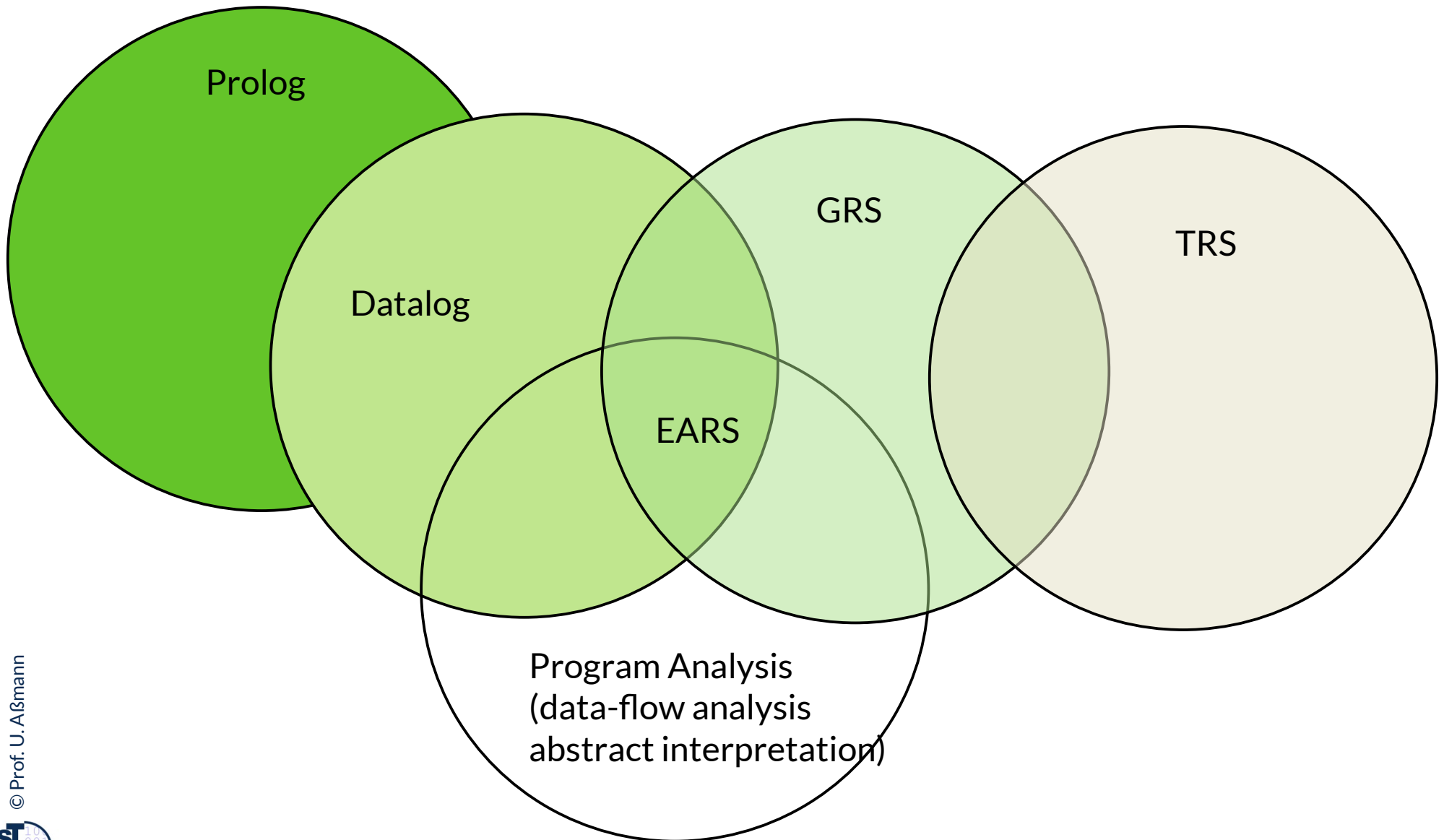
```
// Transitive Closure in ATL, with a recursive OCL query
rule computeTransitiveClosureBaseCase {
  from node: Node (
    // possible to call OCL expressions
    node->baserelation.collect( e | e.baserelation)->flatten() );
  )
  to newNode mapsTo node (
    // set new transitive relation
    newNode->transitiverelation <- node->baserelation
  )
}
rule computeTransitiveClosureRecursiveCase {
  from node: Node (
    node->transitiverelation.collect( e | e.baserelation)->flatten() );
  )
  to newNode mapsTo node (
    // set new transitive relation
    newNode->transitiverelation <- node->transitiverelation
  )
}
```

32.5 More on the Logic-Graph Isomorphism

Results

- ▶ Theory: Graph rewriting, DATALOG and data-flow analysis have a common core:
 - EARS build the bridge between graph analysis and transformations
- ▶ Exhaustive GRS: If a termination graph can be identified, a graph rewrite systems terminates.
- ▶ Program optimization:
 - Spezifikation of program optimizations is possible with graph rewrite systems. Short specifications, fewer effort.
 - Practically usable optimizer components can be generated.
- ▶ Uniform Specification of Analysis and Transformation
 - If the program analysis (including abstract interpretation) is specified with GRS
 - It can be unified with program transformation
- ▶ Limitations
 - Several optimizations can be specified with GRS which are not exhaustive (peephole optimization, constant propagation with partial evaluation).
 - As general rule embedding is not allowed, a rule only matches a fixed number of nodes.

The Common Core of Logic, Rewriting and Program Analysis



There clearly remains more work to be done in the following areas:

- ▶ **discovery of other properties of transformations that appear to have relevance to code optimization,**
- ▶ **development of simple tests of these properties, and**
- ▶ **the use of these properties to construct efficient and effective optimization algorithms that apply the transformations involved.**

Aho, Sethi, Ullmann in Code Optimization and Finite Church-Rosser Systems, 1972

The End

- ▶ Explain a connected graph pattern for local graph rewriting. What is a disconnected graph pattern for context-sensitive graph rewriting?
- ▶ What does it mean when GRS are exhaustive (XGRS)?

Terminology for Automated Graph Rewriting

- ▶ **Graph rewrite rule:** rule (left, right hand side) to match left-hand side in the graph and to transform it to the right-hand side
- ▶ **Graph rewrite system:** set of graph rewrite rules
- ▶ **Start graph (axiom):** input graph to rewriting
- ▶ **Graph rewrite problem:** a graph rewrite system applied to a start graph
- ▶ **Manipulated graph (host graph):** graph which is rewritten in graph rewrite problem
- ▶ **Redex:** (reducible expression) application place of a rule in the manipulated graph
- ▶ **Derivation:** a sequence of rewrite steps on the manipulated graph, starting from the start graph and ending in the normal form
- ▶ **Normal form:** result graph of rewriting; manipulated graphs without further redex
- ▶ **Unique normal form:** unique result of a rewrite system, applied to one start graph
- ▶ **Terminating GRS:** rewrite system that stops after finite number of rewrites
- ▶ **Confluent GRS:** two derivations always can be commuted, resp. joined together to one result
- ▶ **Convergent GRS:** rewrite system that always yields unique results (terminating and confluent)